



Subject card

|   |   |  |  |                                     |  |                                       |  |  |
|---|---|--|--|-------------------------------------|--|---------------------------------------|--|--|
| Subject name and code   | Mathematics I, PG_00039849  |  |  |                                     |  |                                       |  |  |
| Field of study  | Mechanical Engineering, Mechanical Engineering  |  |  |                                     |  |                                       |  |  |
| Date of commencement of studies   | October 2020  |  | Academic year of realisation of subject  |                                     | 2020/2021                                      |                                       |  |  |
| Education level   | first-cycle studies   |  | Subject group  |                                     | Obligatory subject group in the field of study |                                       |  |  |
| Mode of study   | Full-time studies   |  | Mode of delivery   |                                     | at the university                              |                                       |  |  |
| Year of study   | 1   |  | Language of instruction  |                                     | Polish   |                                       |  |  |
| Semester of study   | 1   |  | ECTS credits   |                                     | 7.0  |                                       |  |  |
| Learning profile  | general academic profile  |  | Assessment form  |                                     | exam   |                                       |  |  |
| Conducting unit   | Mathematics Center -> Vice-Rector for Education   |  |  |                                     |  |                                       |  |  |
| Name and surname of lecturer (lecturers)  | Subject supervisor  |  | dr Stanisław Domachowski   |                                     |  |                                       |  |  |
|   | Teachers  |  | dr Stanisław Domachowski<br><br>mgr Mirosław Bednarczyk  |                                     |  |                                       |  |  |
| Lesson types and methods of instruction   | Lesson type   | Lecture  | Tutorial   | Laboratory                          | Project  | Seminar                               |  |  |
|   | Number of study hours   | 30.0   | 45.0   | 0.0                                 | 0.0  | 75                                    |  |  |
|   | E-learning hours included: 0.0  |  |  |                                     |  |                                       |  |  |
| Adresy na platformie eNauczanie:<br>WM - MiBM - MATEMATYKA I 2020/21 (S.Domachowski) - Moodle ID: 9839<br><a href="https://enauczanie.pg.edu.pl/moodle/course/view.php?id=9839">https://enauczanie.pg.edu.pl/moodle/course/view.php?id=9839</a> |   |  |  |                                     |  |                                       |  |  |
| Learning activity and number of study hours   | Learning activity   | Participation in didactic classes included in study plan |  | Participation in consultation hours |  | SUM                                   |  |  |
|   | Number of study hours   | 75   |  | 7.0                                 |  | 93.0                                  |  |  |
|   |   | 175  |  |                                     |  |                                       |  |  |
| Subject objectives  | The aim of this subject is for the student to obtain the competence in the range of using basic methods of mathematical analysis and linear algebra. Furthermore, the student is able to use this knowledge to solve simple theoretical and practical problems that can be found in the field of engineering. |  |  |                                     |  |                                       |  |  |
| Learning outcomes   | Course outcome  |  | Subject outcome  |                                     |  | Method of verification                |  |  |
|   | [K6_W01] possesses mathematical knowledge within the range of linear algebra and mathematical analysis useful in characterising and interpreting mechanical systems, technological processes and operational properties of devices  |  | Student defines the basic concepts of differential calculus of one variable. Student analyses the properties of functions on the basis of an examination of its first and second derivatives. Student geometrically interprets the results of an examination of a graph of a function using the concept of limit, continuity and derivatives of functions. Student applies the basic rules and techniques of integration to calculate indefinite integrals. Student lists geometrical applications of definite integrals. Student distinguishes between types of improper integrals. Student studies convergence of number series. |                                     |  | [SW1] Assessment of factual knowledge |  |  |
|   | [K6_U01] is able to acquire information from specialized literary sources, databases and other resources, essential for solving engineering tasks; is able to compile the obtained information pieces and to interpret them, additionally is able to form conclusions and present justified opinion           |  |  |                                     |  |                                       |  |  |

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|--|---|-------------------|-------------------------------|
| Subject contents   | Functions of one variable and their properties: The absolute value function – definition, solving equations and inequalities with absolute value, graphs of functions with absolute value. Power functions – solving power and polynomial equations and inequalities. Rational functions – solving rational equations and inequalities. Exponential function – properties and graphs, solving exponential equations and inequalities. Logarithmic functions – properties and graphs, solving logarithmic equations and inequalities. Trigonometric and cyclometric functions – properties and graphs, solving trigonometric equations and inequalities. Infinite sequences. Fundamental definitions of a limit of a sequence, convergence and divergence, limit theorems. Applications to solving equation. Differential calculus of one variable functions and its applications: Definition of a first derivative and differential. Roll's and Lagrange's theorems. Higher derivatives and differentials. Monotonicity and local extrema. Convexity, concavity and inflection points of a function. De l'Hospital's Thorem. Asymptotes. Applying differential calculus to studying the properties of one variable functions. Integral calculus of one variable functions – antiderivatives: The process of finding antiderivatives and integration formulas – the substitution method of integration and integration by parts. Integration of rational, trigonometric and irrational functions. Definite integrals in Riemann's sense: Newton-Leibniz Thorem. Integration formulas, the substitution method of integration and integration by parts for definite integrals. Applications of integral calculus in computing areas of plane figures, lengths of arcs, volumes of solids of revolution. Improper integrals, applications of improper integrals. Improper integrals, applications of improper integrals.   |                   |                               |
| Prerequisites and co-requisites  |   |                   |                               |
| Assessment methods and criteria  | Subject passing criteria  | Passing threshold | Percentage of the final grade |
| written exam 90 minutes, tests, etest, • Active participation during classes | 50.0%   | 100.0%            |                               |
| Recommended reading  | <p>Basic literature</p> <p>W.Żakowski, G.Decewicz , Matematyka część 1 Analiza Matematyczna, Wydawnictwa Naukowo- Techniczne, Warszawa 1991, B.Wikiel, Matematyka, Podstawy z elementami matematyki wyższej, Wydawnictwo Politechniki Gdańskie Gdańsk 2009, W. Krysicki, L. Włodarski „Analiza matematyczna w zadaniach” część I, PWN, Warszawa 1986 W. Stankiewicz „Zadania z matematyki dla wyższych uczelni technicznych”, cz.I, PWN, Warszawa 1980,K.Jankowska, J.Jankowski, Zbiór zadań z matematyki, Wydawnictwo Politechniki Gdańskie Gdańsk 2003. J.Dymkowska, D. Beger „Rachunek całkowy w zadaniach” Wydawnictwo Politechniki Gdańskie Gdańsk 2015, J.Dymkowska, D. Beger „Rachunek różniczkowy w zadaniach” Wydawnictwo Politechniki Gdańskie Gdańsk 2015,</p> <p>Supplementary literature</p> <p>A. Kielbasa "Matematyka Matura 2009 Matura 2010 poziom podstawowy i rozszerzony" cz. I i II, Wyd. "2000", Warszawa 2008 Z. Cewe, J. Kobierska, H. Nahorska, I. Stepuro, J. Witkowska "Matura z matematyki od roku 2010", Zbiór zadań maturalnych z zakresu kształcenia rozszerzonego, Wydawnictwo "Podkowa", Gdańsk 2010W. Jankowski „Matematyka. Podręcznik dla wydziałów elektrycznych i mechanicznych politechnik”, PWN, Warszawa 1967 W. Leksiński, I. Nabiałek, W. Żakowski „Matematyka. Definicje, twierdzenia, przykłady, zadania”-podręczniki akademickie , Wyd. NT, Warszawa 1994, K.Dobrowolska, praca zbiorowa „Matematyka dla studiów technicznych dla pracujących” Tom I, PWN, Warszawa 1981, R. Grzymkowski „Matematyka, zadania i odpowiedzi”, podręczniki akademickie, Wyd. Pracowni Komputerowej Jacka Skalmierskiego, Gliwice 2002 M. Gewert, Z. Skoczyłas „Analiza matematyczna 1, Przykłady i zadania”, Oficyna Wydawnicza Gis, Wrocław 2005 J. Głazunow „Matematyka wyższa, zbiór zadań z analizy funkcji jednej zmiennej”, Wyd. Elbląskiej Uczelni Humanistyczno-Ekonomicznej, Elbląg 2006 M. Lassak „Zadania z analizy matematycznej”, Wyd. Wspierania Procesu Edukacji, Warszawa 2003</p> <p>eResources addresses</p> <p>WM - MiBM - MATEMATYKA I 2020/21 (S.Domachowski) - Moodle ID: 9839<br/> <a href="https://enauuczanie.pg.edu.pl/moodle/course/view.php?id=9839">https://enauuczanie.pg.edu.pl/moodle/course/view.php?id=9839</a></p> |                   |                               |
| Example issues/example questions/tasks being completed                       | <p>1.Find the domain and the set of values of the function <math>f(x)=\log_2(x+2)</math>.</p> <p>2.Solve the equation <math> x-3 ^2 - 4 x-3  - 12 = 0</math>.</p> <p>3. Solve the inequality: <math>36x^4 - 97x^2 + 36 &lt; 0</math> .</p> <p>4.Solve the equation: <math>11 \cdot 52x - 4x = 3 \cdot 22x + 25x</math>.</p> <p>5.Solve the inequality: <math>\log_2(x+6) \geq 1</math>.</p> <p>6.Solve the equation: <math> \cos x  = \cos x + 2 \sin x</math>.</p> <p>7.Find the domain and the set of values of the function <math>f(x)=\log_2(x+2)</math>. Determine the inverse function of f.</p> <p>8. Evaluate the limit of a given sequence <math>a_n = (3n^2 + 6n)^{1/2} - 3^{1/2} n</math>.</p> <p>9. Evaluate the indefinite integral of the given rational function <math>f(x) = (x+3)/(x^3 + 3x^2 + 4x + 2)</math>.</p> <p>10.Find local extremes and intervals of monotonicity of the following function <math>f(x) = (x^2 + 4x + 1)e^x</math>.</p>   |                   |                               |
| Work placement   | Not applicable  |                   |                               |