



Subject card

Subject name and code	Mathematics II, PG_00044683						
Field of study	Civil Engineering						
Date of commencement of studies	October 2020		Academic year of realisation of subject		2020/2021		
Education level	first-cycle studies		Subject group		Obligatory subject group in the field of study		
Mode of study	Part-time studies		Mode of delivery		at the university		
Year of study	1		Language of instruction		Polish		
Semester of study	2		ECTS credits		8.0		
Learning profile	general academic profile		Assessment form		exam		
Conducting unit	Mathematics Center -> Vice-Rector for Education						
Name and surname of lecturer (lecturers)	Subject supervisor		dr Krzysztof Radziszewski				
	Teachers		mgr inż. Krystyna Dąbrowska dr Krzysztof Radziszewski				
Lesson types and methods of instruction	Lesson type	Lecture	Tutorial	Laboratory	Project	Seminar	SUM
	Number of study hours	30.0	30.0	0.0	0.0	0.0	60
	E-learning hours included: 0.0						
	Adresy na platformie eNauczanie: WILiŚ - Bud. IŚ niestacjonarne sem.2 - Matematyka 2020/2021 (K.Radziszewski) - Moodle ID: 13624 https://enauczanie.pg.edu.pl/moodle/course/view.php?id=13624 WILiŚ - Bud. IŚ niestacjonarne sem.2 - Matematyka 2020/2021 (K.Radziszewski) - Moodle ID: 13624 https://enauczanie.pg.edu.pl/moodle/course/view.php?id=13624 WILiŚ - Bud. IŚ niestacjonarne sem.2 - Matematyka 2020/2021 (K.Radziszewski) - Moodle ID: 13624 https://enauczanie.pg.edu.pl/moodle/course/view.php?id=13624						
Learning activity and number of study hours	Learning activity	Participation in didactic classes included in study plan		Participation in consultation hours		Self-study	SUM
	Number of study hours	60		7.0		133.0	200
Subject objectives	Students obtain competence in the range of using methods of mathematical analysis and knowledge how to solve simple problems that can be found in the field of engineering.						

Learning outcomes	Course outcome	Subject outcome	Method of verification
	[K6_W01] has knowledge of selected branches of mathematics, physics and chemistry, which is a base of construction subjects, such as construction theory and material technology and is needed to formulate and solve typical problems of civil engineering	Student lists geometrical applications of definite integrals. Student distinguishes between types of improper integrals. Student uses definite integral to solve geometrical tasks. Student computes partial derivatives and uses differential calculus to examine properties of the function of several variables. Student uses the basic operations on complex numbers. Student solves ordinary differential equations. Student computes multiple integrals and uses integral calculus to geometric and mechanics applications. Student computes the gradient of a scalar field, divergence and rotation of a vector field and a potential field. Student studies convergence of number series. Student calculates the radius of convergence and the interval of convergence of a power series. Student uses power series in order to compute sums of number series. Student calculates the probability of random events. Student describes the basic types of distributions of random variable. Student gives the definition of basic notions of probability theory.	[SW1] Assessment of factual knowledge
	[K6_U02] is able to define basic calculation models used in computer calculations	Student solves equations and inequalities with elementary functions. Student defines basic notions of differential calculus of one variable function. Student determines intervals of monotonicity of a given functions and its extrema. Student applies the basic rules and techniques of integration to calculate indefinite. Student lists geometrical applications of definite integrals. Student distinguishes between types of improper integrals. Student uses definite integral to solve geometrical tasks. Student recognizes the importance of skillful use of basic mathematical apparatus in terms of study in future.	[SU2] Assessment of ability to analyse information

Subject contents	<p>Definite integrals in Riemann's sense: Newtona-Leibniza Thorem. Methods of evaluations of definite integrals. Applications of definite integrals. Improper integrals. Applications of improper integrals. Integration formulas, the substitution method of integration and integration by parts for definite integrals. Applications of integral calculus in computing areas of plane figures, lengths of arcs, volumes of solids of revolution.</p> <p>Functions of several variables: Limit and continuity of a function of several variables. Partial derivatives. Total differential. Taylor's formula. Maxima and minima of a function of several variables. Implicit functions.</p> <p>Complex numbers: Algebraic, trigonometric, exponential form, operations, exponentiation (Moivre formula), finding roots of complex numbers. Operations on complex numbers.</p> <p>Ordinary differential equations: First order differential equations. General and particular solution. The Cauchy initial value problem. Variables separable, linear, Bernoulli, exact differential equations. Second order linear differential equations with constant coefficients. Fundamental set of solution of the homogeneous linear differential equation. Non-homogeneous linear differential equations. Higher order linear differential equations with constant coefficients. Double and triple integrals. Applications of multiple integrals. Line integrals with applications.</p> <p>Elements of field theory and differential geometry: Scalar and vector fields, the gradient of a scalar field, divergence and rotation of a vector field, a potential field. Line integrals with applications.</p> <p>Number series and function series: Number series. Convergent and divergent series. Convergence tests of the number series. Power series. Radius and interval of convergence. Integration and differentiation of power series. Examples of applications - approximate calculation of integrals.</p> <p>Calculus of probability: Discrete and continuous random variables, distribution function, expected value and variance of a random variable. Basic distribution of random variables.</p>		
Prerequisites and co-requisites	No requirements		
Assessment methods and criteria	Subject passing criteria	Passing threshold	Percentage of the final grade
	Midterm colloquium	50.0%	40.0%
	Written exam	50.0%	60.0%
Recommended reading	Basic literature	K. Jankowska, T. Jankowski, Funkcje wielu zmiennych. Całki wielokrotne. Geometria analityczna, PG, Gdańsk 2005. K. Jankowska, T. Jankowski, Zadania z matematyki wyższej, PG, Gdańsk 1999. W. Kryszicki, L. Włodarski, Analiza matematyczna w zadaniach I i II, Wydawnictwo Naukowe PWN, Warszawa 1998. E. Pluciński, Elementy probabilistyki, Wydawnictwo Naukowe PWN, Warszawa 1981.	
	Supplementary literature	E. Mieloszyk, Liczby zespolone, PG, Gdańsk 2003. M. Gewert, Z. Skoczylas, Analiza matematyczna 2 – Definicje, twierdzenia, wzory, Oficyna Wydawnicza GiS, Wrocław 2003. M. Gewert, Z. Skoczylas, Analiza matematyczna 2 – Przykłady i zadania, Oficyna Wydawnicza GiS, Wrocław 2003. M. Gewert, Z. Skoczylas, Równania różniczkowe zwyczajne, Oficyna Wydawnicza GiS, Wrocław 2001. R. Leitner, Zarys matematyki wyższej I i II, Wydawnictwo Naukowo-Techniczne, Warszawa 2001. R. Leitner, W. Matuszewski, Z. Rojek, Zadania z matematyki wyższej I i II, Wydawnictwo Naukowo-Techniczne, Warszawa 1999.	
	eResources addresses	WLiŚ - Bud. IŚ niestacjonarne sem.2 - Matematyka 2020/2021 (K.Radziszewski) - Moodle ID: 13624 https://enauczanie.pg.edu.pl/moodle/course/view.php?id=13624 WLiŚ - Bud. IŚ niestacjonarne sem.2 - Matematyka 2020/2021 (K.Radziszewski) - Moodle ID: 13624 https://enauczanie.pg.edu.pl/moodle/course/view.php?id=13624 WLiŚ - Bud. IŚ niestacjonarne sem.2 - Matematyka 2020/2021 (K.Radziszewski) - Moodle ID: 13624 https://enauczanie.pg.edu.pl/moodle/course/view.php?id=13624	

Example issues/ example questions/ tasks being completed	<ol style="list-style-type: none"> 1. Find the area between the two curves $y=e^x$ and $y=3-e^x$ from $x=-2$ to $x=0$. 2. Sketch the graph of the function $f(x,y)=x^2$. 3. Identify any local extrema of the function $f(x,y)=e^x-y(x^2-2y^2)$. 4. Find the absolute extrema of the function $f(x,y)=xy-x(x+1)-y(y+1)$ on the set $D=\{(x,y): x^2+y^2\leq 25, y\geq 3\}$. 5. Solve the equation $y''+6y'+9y=10\sin x$. 6. Find the divergence and rotation of the vector field $[2xe^{3y}+z^2, 3x^2e^{3y}+z, 2zx+y]$. 7. Find the distribution function, expected value and variance of a random variable X: $P(-2)=0,1$, $P(-1)=0,5$, $P(0)=0,2$, $P(3)=0,1=P(5)$.
Work placement	Not applicable