



Subject card

Subject name and code	Linear algebra with geometry, PG_00034519						
Field of study	Technical Physics						
Date of commencement of studies	October 2021	Academic year of realisation of subject			2021/2022		
Education level	first-cycle studies	Subject group			Obligatory subject group in the field of study Subject group related to scientific research in the field of study		
Mode of study	Full-time studies	Mode of delivery			at the university		
Year of study	1	Language of instruction			Polish		
Semester of study	2	ECTS credits			5.0		
Learning profile	general academic profile	Assessment form			exam		
Conducting unit	Department of Probability Theory and Biomathematics -> Faculty of Applied Physics and Mathematics						
Name and surname of lecturer (lecturers)	Subject supervisor		dr Joanna Cyman				
	Teachers		dr Joanna Cyman				
Lesson types and methods of instruction	Lesson type	Lecture	Tutorial	Laboratory	Project	Seminar	SUM
	Number of study hours	30.0	30.0	0.0	0.0	0.0	60
	E-learning hours included: 0.0 Adresy na platformie eNauczanie: Algebra liniowa 2022 - Moodle ID: 18617 https://enauczanie.pg.edu.pl/moodle/course/view.php?id=18617						
Learning activity and number of study hours	Learning activity	Participation in didactic classes included in study plan	Participation in consultation hours	Self-study	SUM		
	Number of study hours	60	5.0	60.0	125		
Subject objectives	Getting to know the basic knowledge in the field of linear algebra and analytic geometry.						
Learning outcomes	Course outcome	Subject outcome			Method of verification		
	K6_W03	Student has basic knowledge in the field of linear algebra and analytical geometry; knows complex numbers, matrix calculus, vector algebra. He knows different methods of solving problems with complex numbers, matrices, solving systems of linear equations and methods of analytic geometry in space R^3 , in the scope necessary in the work of an engineer.			[SW1] Assessment of factual knowledge		
	K6_U01	A student understands the value independent development of knowledge. He independently solves exercises that consolidate knowledge.			[SU2] Assessment of ability to analyse information		

Subject contents	<p>Complex numbers. Operations on complex numbers. Solving algebraic equations in the complex space. Different forms of a complex number. Geometric interpretation, Gaussian plane. Exponentiation, nth root. The basic theorem of algebra.</p> <p>Matrix calculus. Matrix operations.. Determinants. Laplace expansion. Inverse matrix. Row of matrices, elementary transformations of matrix. Systems of linear equations. Cramer's rule. The existence of solutions of the system of linear equations, the Kronecker-Capelli theorem.</p> <p>Analytic geometry in space.Vectors. Scalar product, orthogonal vectors. Vector product, mixed product and its geometric interpretation. Equations of plane and line in R^3. Conical curves.</p> <p>Vector space. The base and dimension of space. Linear transformations. The kernel and image of transformation. Linear transformation matrix. Values and eigenvectors. Euclidean spaces. Gram–Schmidt process.</p>														
Prerequisites and co-requisites	Basic knowledge of mathematics in the field of secondary school.														
Assessment methods and criteria	<table border="1" data-bbox="448 584 1487 723"> <thead> <tr> <th data-bbox="448 584 794 618">Subject passing criteria</th> <th data-bbox="794 584 1141 618">Passing threshold</th> <th data-bbox="1141 584 1487 618">Percentage of the final grade</th> </tr> </thead> <tbody> <tr> <td data-bbox="448 618 794 651">egzamination</td> <td data-bbox="794 618 1141 651">50.0%</td> <td data-bbox="1141 618 1487 651">40.0%</td> </tr> <tr> <td data-bbox="448 651 794 685">colloquia</td> <td data-bbox="794 651 1141 685">50.0%</td> <td data-bbox="1141 651 1487 685">54.0%</td> </tr> <tr> <td data-bbox="448 685 794 723">exercises</td> <td data-bbox="794 685 1141 723">50.0%</td> <td data-bbox="1141 685 1487 723">6.0%</td> </tr> </tbody> </table>			Subject passing criteria	Passing threshold	Percentage of the final grade	egzamination	50.0%	40.0%	colloquia	50.0%	54.0%	exercises	50.0%	6.0%
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Example issues/ example questions/ tasks being completed	1.Mark on the complex plane the set described by inequality: $2 < (3+4i)z+i < 3$. 2.Solve a system of equations: $4x+y+3z-t=5$ $2x-y+3z+2t=2$ $3x+y+2z-t=1$ $5x+y+4z+2t=0$.														
Work placement	Not applicable														