



## Subject card

|                                             |                                                                                                                                                                                                                        |                                                          |                                                                                                                                                                                                                                                                                                                                                                        |                                     |                                                                                                                      |            |     |
|---------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------|----------------------------------------------------------------------------------------------------------------------|------------|-----|
| Subject name and code                       | Linear algebra with geometry, PG_00034519                                                                                                                                                                              |                                                          |                                                                                                                                                                                                                                                                                                                                                                        |                                     |                                                                                                                      |            |     |
| Field of study                              | Technical Physics                                                                                                                                                                                                      |                                                          |                                                                                                                                                                                                                                                                                                                                                                        |                                     |                                                                                                                      |            |     |
| Date of commencement of studies             | October 2021                                                                                                                                                                                                           |                                                          | Academic year of realisation of subject                                                                                                                                                                                                                                                                                                                                |                                     | 2021/2022                                                                                                            |            |     |
| Education level                             | first-cycle studies                                                                                                                                                                                                    |                                                          | Subject group                                                                                                                                                                                                                                                                                                                                                          |                                     | Obligatory subject group in the field of study<br>Subject group related to scientific research in the field of study |            |     |
| Mode of study                               | Full-time studies                                                                                                                                                                                                      |                                                          | Mode of delivery                                                                                                                                                                                                                                                                                                                                                       |                                     | at the university                                                                                                    |            |     |
| Year of study                               | 1                                                                                                                                                                                                                      |                                                          | Language of instruction                                                                                                                                                                                                                                                                                                                                                |                                     | Polish                                                                                                               |            |     |
| Semester of study                           | 2                                                                                                                                                                                                                      |                                                          | ECTS credits                                                                                                                                                                                                                                                                                                                                                           |                                     | 5.0                                                                                                                  |            |     |
| Learning profile                            | general academic profile                                                                                                                                                                                               |                                                          | Assessment form                                                                                                                                                                                                                                                                                                                                                        |                                     | exam                                                                                                                 |            |     |
| Conducting unit                             | Department of Probability Theory and Biomathematics -> Faculty of Applied Physics and Mathematics                                                                                                                      |                                                          |                                                                                                                                                                                                                                                                                                                                                                        |                                     |                                                                                                                      |            |     |
| Name and surname of lecturer (lecturers)    | Subject supervisor                                                                                                                                                                                                     |                                                          | dr Joanna Cyman                                                                                                                                                                                                                                                                                                                                                        |                                     |                                                                                                                      |            |     |
|                                             | Teachers                                                                                                                                                                                                               |                                                          | dr Joanna Cyman                                                                                                                                                                                                                                                                                                                                                        |                                     |                                                                                                                      |            |     |
| Lesson types and methods of instruction     | Lesson type                                                                                                                                                                                                            | Lecture                                                  | Tutorial                                                                                                                                                                                                                                                                                                                                                               | Laboratory                          | Project                                                                                                              | Seminar    | SUM |
|                                             | Number of study hours                                                                                                                                                                                                  | 30.0                                                     | 30.0                                                                                                                                                                                                                                                                                                                                                                   | 0.0                                 | 0.0                                                                                                                  | 0.0        | 60  |
|                                             | E-learning hours included: 0.0                                                                                                                                                                                         |                                                          |                                                                                                                                                                                                                                                                                                                                                                        |                                     |                                                                                                                      |            |     |
|                                             | Adresy na platformie eNauczanie:<br>Algebra liniowa 2022 - Moodle ID: 18617<br><a href="https://enauczanie.pg.edu.pl/moodle/course/view.php?id=18617">https://enauczanie.pg.edu.pl/moodle/course/view.php?id=18617</a> |                                                          |                                                                                                                                                                                                                                                                                                                                                                        |                                     |                                                                                                                      |            |     |
| Learning activity and number of study hours | Learning activity                                                                                                                                                                                                      | Participation in didactic classes included in study plan |                                                                                                                                                                                                                                                                                                                                                                        | Participation in consultation hours |                                                                                                                      | Self-study | SUM |
|                                             | Number of study hours                                                                                                                                                                                                  | 60                                                       |                                                                                                                                                                                                                                                                                                                                                                        | 5.0                                 |                                                                                                                      | 60.0       | 125 |
| Subject objectives                          | Getting to know the basic knowledge in the field of linear algebra and analytic geometry.                                                                                                                              |                                                          |                                                                                                                                                                                                                                                                                                                                                                        |                                     |                                                                                                                      |            |     |
| Learning outcomes                           | Course outcome                                                                                                                                                                                                         |                                                          | Subject outcome                                                                                                                                                                                                                                                                                                                                                        |                                     | Method of verification                                                                                               |            |     |
|                                             | K6_W03                                                                                                                                                                                                                 |                                                          | Student has basic knowledge in the field of linear algebra and analytical geometry; knows complex numbers, matrix calculus, vector algebra.<br>He knows different methods of solving problems with complex numbers, matrices, solving systems of linear equations and methods of analytic geometry in space $R^3$ , in the scope necessary in the work of an engineer. |                                     | [SW1] Assessment of factual knowledge                                                                                |            |     |
|                                             | K6_U01                                                                                                                                                                                                                 |                                                          | A student understands the value independent development of knowledge.<br><br>He independently solves exercises that consolidate knowledge.                                                                                                                                                                                                                             |                                     | [SU2] Assessment of ability to analyse information                                                                   |            |     |

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| Subject contents                                               | <p><b>Complex numbers.</b> Operations on complex numbers. Solving algebraic equations in the complex space. Different forms of a complex number. Geometric interpretation, Gaussian plane. Exponentiation, nth root. The basic theorem of algebra.</p> <p><b>Matrix calculus.</b> Matrix operations.. Determinants. Laplace expansion. Inverse matrix. Row of matrices, elementary transformations of matrix. Systems of linear equations. Cramer's rule. The existence of solutions of the system of linear equations, the Kronecker-Capelli theorem.</p> <p><b>Analytic geometry in space.</b>Vectors. Scalar product, orthogonal vectors. Vector product, mixed product and its geometric interpretation. Equations of plane and line in <math>\mathbb{R}^3</math>. Conical curves.</p> <p><b>Vector space.</b> The base and dimension of space. Linear transformations. The kernel and image of transformation. Linear transformation matrix. Values and eigenvectors. Euclidean spaces. Gram–Schmidt process.</p> |                                                                                                                                                                                                                                                                                                                                                                                                                                                                 |                               |
| Prerequisites and co-requisites                                | Basic knowledge of mathematics in the field of secondary school.                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       |                                                                                                                                                                                                                                                                                                                                                                                                                                                                 |                               |
| Assessment methods and criteria                                | Subject passing criteria                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               | Passing threshold                                                                                                                                                                                                                                                                                                                                                                                                                                               | Percentage of the final grade |
|                                                                | egzamination                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | 50.0%                                                                                                                                                                                                                                                                                                                                                                                                                                                           | 40.0%                         |
|                                                                | colloquia                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              | 50.0%                                                                                                                                                                                                                                                                                                                                                                                                                                                           | 54.0%                         |
|                                                                | exercises                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              | 50.0%                                                                                                                                                                                                                                                                                                                                                                                                                                                           | 6.0%                          |
| Recommended reading                                            | Basic literature                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       | 1. T. Jurlewicz, Z. Skoczylas, Algebra liniowa 1 i 2. Definicje, twierdzenia, wzory, Oficyna Wydawnicza GiS, Wrocław 2012.<br><br>2. T. Jurlewicz, Z. Skoczylas, Algebra liniowa 1 i 2. Przykłady i zadania, Oficyna Wydawnicza GiS, Wrocław 2012.<br><br>3. J. Topp, Algebra liniowa, Wydawnictwo Uniwersytetu Gdańskiego, Gdańsk 2015.<br><br>4. Donald A. McQuarrie, Matematyka dla przyrodników i inżynierów Tom 1, Wydawnictwo Naukowe PWN, Warszawa 2018. |                               |
|                                                                | Supplementary literature                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               | 1. L. Kowalski, Elementy algebry liniowej z geometrią analityczną dla informatyków, Bel Studio, 2005.<br><br>2. G. Banaszak, W. Gajda, Elementy algebry liniowej I, II, WNT, Warszawa 2002.                                                                                                                                                                                                                                                                     |                               |
|                                                                | eResources addresses                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | Algebra liniowa 2022 - Moodle ID: 18617<br><a href="https://enauczanie.pg.edu.pl/moodle/course/view.php?id=18617">https://enauczanie.pg.edu.pl/moodle/course/view.php?id=18617</a>                                                                                                                                                                                                                                                                              |                               |
| Example issues/<br>example questions/<br>tasks being completed | 1.Mark on the complex plane the set described by inequality: $2 <  (3+4i)z+i  < 3$ .<br>2.Solve a system of equations:<br>$4x+y+3z-t=5$<br>$2x-y+3z+2t=2$<br>$3x+y+2z-t=1$<br>$5x+y+4z+2t=0$ .                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         |                                                                                                                                                                                                                                                                                                                                                                                                                                                                 |                               |
| Work placement                                                 | Not applicable                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         |                                                                                                                                                                                                                                                                                                                                                                                                                                                                 |                               |