GDAŃSK UNIVERSITY OF TECHNOLOGY

Subject card

Subject name and code	Probability Theory, PG_00025511					
Field of study	Mathematics					
Date of commencement of studies	October 2021		Academic year of realisation of subject	2023/2024		
Education level	first-cycle studies		Subject group	Obligatory subject group in the field of study		
				Subject group related to scientific research in the field of study		
Mode of study	Full-time studies		Mode of delivery	at the university		
Year of study	3		Language of instruction	Polish		
Semester of study	5		ECTS credits	5.0		
Learning profile	general academic profile		Assessment form	exam		
Conducting unit	Department of Probability Theory and Biomathematics -> Faculty of Applied Physics and Mathematics					
Name and surname of lecturer (lecturers)	Subject supervisor	prof. dr hab. inż. Tomasz Szarek				
	Teachers	mgr inż. Katarzyna Tessmer				
		prof. dr hab. inż. Tomasz Szarek				

Lesson types and methods of instruction	Lesson type	Lecture	Tutorial	Laboratory	Project	Seminar	SUM
	Number of study hours	30.0	30.0	0.0	0.0	0.0	60
	E-learning hours included: 0.0						

Learning activity and number of study hours	Learning activity	Participation in didactic classes included in study plan	Participation in consultation hours	Self-study	SUM
	Number of study hours	60	5.0	60.0	125

Subject objectives	Introduction to basic notions of modern probability based on measure theory. Equipping a student in the knowledge necessary for uderstanding randomness and relevant interaction with the surrounding environment and sociopolitical reality.

Learning outcomes	Course outcome	Subject outcome	Method of verification
	K6_U03	Constructs probability space to a concrete phenomena. Applies methods of linear algebra and analysis to describe multivariate random effects.	[SU4] Assessment of ability to use methods and tools
	K6_U11	Precisely describes different types of random events using the language of axiomatic probability theory. Distinguishes different types od random variables and evaluates their expectations, variances and other moments. Interprets (in applications)laws of large numbers. Estimates parameters of distributions. Performs statistical inference.	[SU3] Assessment of ability to use knowledge gained from the subject
	K6_W02	Recognizes conditional probability, independence of events and random variables.	[SW1] Assessment of factual knowledge
	K6_W04	Uses methods of logic, analysis, algebra and measure theory in probability.	[SW1] Assessment of factual knowledge
	K6_U02	Explains different nodes of stochastic convergence.	[SU1] Assessment of task fulfilment

Subject contents	LECTURES Radon-Nikodym theorem. Conditional expectation. Regression. Sums of independent random variables. Weak law of large numbers. L^2 law of large numbers. Strong law of large numbers (Kolmogorov, Etemadi). Stationary sequences. Maximal ergodic lemma. Individual ergodic theorem for stationary sequences. Empirical distributions. Glivenko-Cantelli theorem. Weak convergence of measures. Characteristic functions. Central limit theorem. Multivariate Gaussian distributions. Fourier transform of measures on R^n. Descriptive statistics. Point estimators. Confidence intervals. Hypothesis testing. Statistical inferring. TUTORIALS During tutorial classes (closely correlated with lectures) students solve numerical exercises and selected theoretical problems.
Prerequisites and co-requisites	Courses completed: Probability Theory term IV (MAT1013/1)

Assessment methods and criteria	Subject passing criteria	Passing threshold	Percentage of the final grade
	Exam	51.0%	50.0%
	Test 2	51.0%	25.0%
	Test 1	51.0%	25.0%

Recommended reading	Basic literature	J.Jakubowski, R.Sztencel, Wstęp do teorii prawdopodobieństwa, Wydawnictwo SCRIPT, Warszawa, 2012. J.Jacod, P.Protter, Probability Essentials, Springer, Berlin Heidelberg, 2000. W.Feller, Wstęp do rachunku prawdopodobieństwa, t.I i II, PWN, warszawa, 2009.
	Supplementary literature	I.I.Gichman, A.W.Skorochod, Wstęp do teorii procesów stochastycznych, PWN, Warszawa, 1968. P.Billingsley, Prawdopodobieństwo i miara, PWN, Warszawa, 1987. G.Grimmett, D.Stirzaker, Probability and Random Processes, Oxford University Press, 2006. R.Magiera, Modele i metody statystyki matematycznej, GiS, Wrocław, 2002.
	eResources addresses	Adresy na platformie eNauczanie: Rachunek prawdopodobieństwa II 2023/24 - Moodle ID: 33209 https://enauczanie.pg.edu.pl/moodle/course/view.php?id=33209

Example issues/ example questions/ tasks being completed	At the beginning of the term students are provided with the list of problems and exercises to be solved or worked out by themselves. Their solutions are presemted on exercises where students give their comments and suggest improvements. Test problems are based on mentioned lists and exam on topics from lectures. Find conditional expectation with respect to a fixed sigma algebra. Study weak convergence and find the limit distribution foe a given sequence of random variables. Estimate a probability of a random event using the central limit theorem.
Work placement	Not applicable