



Subject card

Subject name and code	Introduction to the measure theory, PG_00021502						
Field of study	Mathematics						
Date of commencement of studies	October 2021		Academic year of realisation of subject		2022/2023		
Education level	first-cycle studies		Subject group		Obligatory subject group in the field of study Subject group related to scientific research in the field of study		
Mode of study	Full-time studies		Mode of delivery		at the university		
Year of study	2		Language of instruction		Polish		
Semester of study	3		ECTS credits		4.0		
Learning profile	general academic profile		Assessment form		assessment		
Conducting unit	Department of Nonlinear Analysis and Statistics -> Faculty of Applied Physics and Mathematics						
Name and surname of lecturer (lecturers)	Subject supervisor		dr hab. Piotr Bartłomiejczyk				
	Teachers		mgr inż. Tomasz Gzella				
			dr hab. Piotr Bartłomiejczyk				
Lesson types and methods of instruction	Lesson type	Lecture	Tutorial	Laboratory	Project	Seminar	SUM
	Number of study hours	15.0	30.0	0.0	0.0	0.0	45
	E-learning hours included: 0.0						
Learning activity and number of study hours	Learning activity	Participation in didactic classes included in study plan		Participation in consultation hours		Self-study	SUM
	Number of study hours	45		5.0		50.0	100
Subject objectives	Equip students with specialized mathematical tools aided for technical subjects.						
Learning outcomes	Course outcome		Subject outcome		Method of verification		
	K6_U06				[SU3] Assessment of ability to use knowledge gained from the subject [SU4] Assessment of ability to use methods and tools		
	K6_W02				[SW1] Assessment of factual knowledge		
	K6_U01				[SU2] Assessment of ability to analyse information		
	K6_U04				[SU4] Assessment of ability to use methods and tools		
	K6_U03				[SU3] Assessment of ability to use knowledge gained from the subject [SU4] Assessment of ability to use methods and tools		
Subject contents	Measure of elementary sets. Jordan measure and its properties. Darboux integral and its properties. Lebesgue measure and its properties. Vitali set. Completeness of measure. Lebesgue integral and its properties. Lusin's theorem. Egorov's theorem. Families of sets, semi-algebras. Measures and their basic properties. Measures on Borel sets. Measurable functions. Integral with respect to measure. Monotone convergence theorem. Fatou lemma. Dominated convergence theorem.						
Prerequisites and co-requisites	set theory, calculus						
Assessment methods and criteria	Subject passing criteria		Passing threshold		Percentage of the final grade		
	Test of lecture		51.0%		50.0%		
	Activity		51.0%		10.0%		
	Colloquium no 1		51.0%		20.0%		
	Colloquium no 2		51.0%		20.0%		

Recommended reading	Basic literature	1) T. Tao, Introduction to measure theorem.
	Supplementary literature	1) P. Billingsley, Probability and measure, . PWN 1979. 2) V. Bogachev, Measure Theory, vol. I, II. Springer 2007. 3) K. Maurin, Analysis, PWN 1973.
	eResources addresses	Adresy na platformie eNauczanie: Wstęp do teorii miary - ćwiczenia 22/23 - Moodle ID: 25788 https://enauczanie.pg.edu.pl/moodle/course/view.php?id=25788 Wstęp do teorii miary - ćwiczenia 22/23 - Moodle ID: 25788 https://enauczanie.pg.edu.pl/moodle/course/view.php?id=25788
Example issues/ example questions/ tasks being completed	<p>Give the definition of Jordan measure and compute the Jordan measure of an arbitrary triangle.</p> <p>Discuss the construction of integrals with respect to measure.</p> <p>Formulate and prove the monotone convergence theorem.</p>	
Work placement	Not applicable	