Subject card

| Subject name and code | Linear Algebra, PG_00047356 |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Field of study | Informatics |  |  |  |  |  |  |
| Date of commencement of studies | October 2021 |  | Academic year of realisation of subject |  |  | 2021/2022 |  |
| Education level | first-cycle studies |  | Subject group |  |  | Obligatory subject group in the field of study <br> Subject group related to scientific research in the field of study |  |
| Mode of study | Full-time studies |  | Mode of delivery |  |  | at the university |  |
| Year of study | 1 |  | Language of instruction |  |  | Polish |  |
| Semester of study | 1 |  | ECTS credits |  |  | 3.0 |  |
| Learning profile | general academic profile |  | Assessment form |  |  | assessment |  |
| Conducting unit | Mathematics Center -> Vice-Rector for Education |  |  |  |  |  |  |
| Name and surname of lecturer (lecturers) | Subject supervisor |  | dr Magdalena Musielak |  |  |  |  |
|  | Teachers |  | dr Magdalena Musielak mgr inż. Dorota Żarek mgr inż. Wojciech Dąbrowski |  |  |  |  |
| Lesson types and methods of instruction | Lesson type | Lecture | Tutorial | Laboratory | Proje | Seminar | SUM |
|  | Number of study hours | 15.0 | 15.0 | 0.0 | 0.0 | 0.0 | 30 |
|  | E-learning hours included: 0.0 |  |  |  |  |  |  |
|  | Adresy na platformie eNauczanie: <br> WETI (Informatyka) - Matematyka 2021/22 (M.Musielak) - Moodle ID: 15372 https://enauczanie.pg.edu.pl/moodle/course/view.php?id=15372 |  |  |  |  |  |  |
| Learning activity and number of study hours | Learning activity | Participation in didactic classes included in study plan |  | Participation in consultation hours |  | Self-study | SUM |
|  | Number of study hours | 30 |  | 3.0 |  | 42.0 | 75 |
| Subject objectives | Students obtain competence in the range of using methods of linear algebra and knowledge how to solve simple problems that can be found in the field of engineering. |  |  |  |  |  |  |


| Learning outcomes | Course outcome | Subject outcome | Method of verification |
| :---: | :---: | :---: | :---: |
|  | [K6_U01] can apply mathematical knowledge to formulate and solve complex and non-typical problems related to the field of study and perform tasks, in an innovative way, in not entirely predictable conditions, by:n- appropriate selection of sources and information obtained from them, assessment, critical analysis and synthesis of this information, $n$ selection and application of appropriate methods and toolsn | Student is able to determine whether a given set with binary operations is an algebraic structure, performs binary operations using modular arithmetic, determines the real and complex roots of polynomials, and performs operations on polynomials using modular arithmetic. Student solves problems in matrix algebra: calculates the determinants, solves matrix equations and systems of linear equations using various methods. Student is able to use scientific software to solve problems from analytical three-dimensional geometry. Student is able to process the acquired information, analyze and interpret it, draw conclusions and reason opinions. | [SU4] Assessment of ability to use methods and tools |
|  | [K6_W01] Knows and understands, to an advanced extent, mathematics necessary to formulate and solve simple issues related to the field of study | Student names the basic algebraic structures, uses the basic operations on complex numbers, knows various methods to solve problems in matrix algebra, is able to determine the number of solutions of a system of equations. Student analyses problems from analytical three-dimensional geometry. <br> Student uses the basic methods of linear algebra to formulate and solve simple problems in the field of informatics | [SW1] Assessment of factual knowledge |
| Subject contents | Binary operations. Groups, rings and fields. Modular arithmetic. <br> Complex numbers. Geometric interpretation. Basic operations. <br> The polynomial ring. Roots of polynomials. Horner's scheme. Fundamental theorem of algebra. <br> Matrices and determinants. Matrix operations. Invertible matrices. Laplace's formula for determinants. <br> Properties of determinants. <br> Methods of matrix inversion. <br> Systems of linear equations. Cramer's theorem. <br> Rank of matrix. Kronecker-Capelly theorem. Gauss-Jordan elimination. <br> Three-dimensional geometry. Cartesian coordinate system. Dot, cross and scalar triple products. Lines and planes in three-dimensional space. |  |  |
| Prerequisites and co-requisites |  |  |  |
| Assessment methods and criteria | Subject passing criteria | Passing threshold | Percentage of the final grade |
|  | Activity | 0.0\% | 10.0\% |
|  | Final test | 50.0\% | 90.0\% |
| Recommended reading | Basic literature | - J. Topp - Algebra liniowa, Wydawn <br> - T. Jurlewicz, Z. Skoczylas - Algebr twierdzenia i wzory., Oficyna wydaw <br> - Jurlewicz, Z. Skoczylas - Algebra zadania., Oficyna wydawnicza GiS, | ictwo PG, 2005 <br> a i geometria analityczna. Definicje, nicza GiS, 2006; geometria analityczna. Przykłady i 2006 |
|  | Supplementary literature | Kajetanowicz P., Wierzejewski analityczna", Wydawnictwo Nauk <br> J. Długosz - Funkcje zespolone | J., ,,Algebra z geometria kowe PWN GiS, 2002 |
|  | eResources addresses | WETI (Informatyka) - Matematyka 15372 <br> https://enauczanie.pg.edu.pl/mood | 2021/22 (M.Musielak) - Moodle ID: e/course/view.php?id=15372 |
| Example issues/ example questions/ tasks being completed | 1. Solve the matrix equation $A X=B$, where $A i B$ are given matrices. <br> 2. Using the Cramer formula find the unknown $y$ from the system of equations : $x+2 y+2 z+3 t=3,3 y+t=1$, $5 x-2 y+t=1,4 x-5 y+2 t=1$. <br> 3. Find all roots of the equation $\mathrm{z} 3-8 \mathrm{i}=0$. Give their algebraic form. <br> 4. Find the linear factorization of the polynomial $W(z)=z 3-i z 2-2 i z-2$, knowing that one of the roots is $z 1=i$. <br> 5. Find the general equation of the plane passing thrugh the point $\mathrm{P}=(1,-1,3)$ and parrarel to the vectors a $=[1,1,0]$ i $b=[0,1,1]$. <br> 6. Discuss the relation between two given lines : $11: x=1+t, y=-2-t, z=3+2 t i l 2$ : $x=4+s, y=-2+2 s, z=4-3 s$. |  |  |
| Work placement | Not applicable |  |  |

