



Subject card

Subject name and code	Risk Processes, PG_00044138						
Field of study	Mathematics						
Date of commencement of studies	October 2022	Academic year of realisation of subject			2022/2023		
Education level	second-cycle studies	Subject group			Optional subject group Subject group related to scientific research in the field of study		
Mode of study	Full-time studies	Mode of delivery			at the university		
Year of study	1	Language of instruction			Polish		
Semester of study	2	ECTS credits			5.0		
Learning profile	general academic profile	Assessment form			exam		
Conducting unit	Zakład Równań Różniczkowych i Zastosowań Matematyki -> Instytut Matematyki Stosowanej -> Faculty of Applied Physics and Mathematics						
Name and surname of lecturer (lecturers)	Subject supervisor	dr Wojciech Czernous					
	Teachers	dr Wojciech Czernous					
Lesson types and methods of instruction	Lesson type	Lecture	Tutorial	Laboratory	Project	Seminar	SUM
	Number of study hours	30.0	0.0	0.0	0.0	30.0	60
E-learning hours included: 0.0							
Learning activity and number of study hours	Learning activity	Participation in didactic classes included in study plan	Participation in consultation hours		Self-study	SUM	
	Number of study hours	60	5.0		60.0	125	
Subject objectives	Introduction to basic mathematical problems related to risk modeling in terms of stochastic (Markov) processes and stochastic differential equations.						
Learning outcomes	Course outcome	Subject outcome			Method of verification		
	K7_W09	Student applies methods of stochastic processes in financial engineering, in particular in modelling insurance risk or survival analysis.			[SW3] Assessment of knowledge contained in written work and projects [SW2] Assessment of knowledge contained in presentation		
	K7_U11	Student poses basic problems related to building appropriate mathematical models of risk processes - in particular ruin processes.			[SU5] Assessment of ability to present the results of task [SU2] Assessment of ability to analyse information		
	K7_K04	Student solves mathematical problems implied by the models of risk, e.g. related to bankruptcy (ruin).			[SK5] Assessment of ability to solve problems that arise in practice		
Learning outcomes	K7_U04	Student analyses continuous-time Markov risk processes.			[SU5] Assessment of ability to present the results of task [SU4] Assessment of ability to use methods and tools		
	Discrete-time Markov processes. Basics of Itô integral. Stochastic differential equations. Standard risk models in terms of stochastic differential equations. The Heath Jarrow Morton model. Reduced form credit risk model. Topics on survival analysis will be presented by students on seminars.						
Prerequisites and co-requisites	Courses completed: Probability Theory, Stochastic Processes						
Assessment methods and criteria	Subject passing criteria		Passing threshold		Percentage of the final grade		
	Project		51.0%		50.0%		
	Exam		51.0%		50.0%		

Recommended reading	Basic literature	<ol style="list-style-type: none"> 1. Jacek Jakubowski, Rafał Sztencel, Wstęp do teorii prawdopodobieństwa. SCRIPT, Warszawa, 2010. 2. Steven E. Shreve, Stochastic Calculus for Finance II. Continuous-Time Models. Springer, 2004. 3. Robert A. Jarrow, Continuous-Time Asset Pricing Theory. A Martingale-Based Approach. Springer, 2018. 4. D.G. Kleinbaum, M. Klein, Survival Analysis, A Self-Learning Text, (3rd Edition), Springer
	Supplementary literature	<ol style="list-style-type: none"> 1. Olav Kallenberg, Foundations of Modern Probability. Springer, 2002. 2. Ioannis Karatzas and Steven E. Shreve. Brownian Motion and Stochastic Calculus. Springer, 1991. 3. Tomasz R. Bielecki, Marek Rutkowski, Credit Risk: Modeling, Valuation and Hedging, Springer, 2004.
	eResources addresses	<p>Adresy na platformie eNauczenie:</p> <p>Procesy ryzyka - Moodle ID: 30552 https://enauczenie.pg.edu.pl/moodle/course/view.php?id=30552</p>
Example issues/ example questions/ tasks being completed	<p>At the beginning of the term the student is provided with the list of topics to be worked out and finally to be presented as a project on a prescribed date. Theoretical components from lectures and seminars are verified on the exam.</p> <p>Give and prove the properties of a homogeneous Markov chain.</p> <p>Give and prove the Doob's theorem on conditional independence.</p> <p>Apply the Itô's formula and find the stochastic differential of the process.</p>	
Work placement	Not applicable	