



Subject card

Subject name and code	, PG_00052289						
Field of study	Mathematics						
Date of commencement of studies	October 2022	Academic year of realisation of subject			2023/2024		
Education level	second-cycle studies	Subject group			Optional subject group Subject group related to scientific research in the field of study		
Mode of study	Full-time studies	Mode of delivery			blended-learning		
Year of study	2	Language of instruction			Polish		
Semester of study	3	ECTS credits			4.0		
Learning profile	general academic profile	Assessment form			assessment		
Conducting unit	Zakład Układów Dynamicznych -> Instytut Matematyki Stosowanej -> Faculty of Applied Physics and Mathematics						
Name and surname of lecturer (lecturers)	Subject supervisor		prof. dr hab. inż. Tomasz Szarek				
	Teachers		prof. dr hab. inż. Tomasz Szarek				
Lesson types and methods of instruction	Lesson type	Lecture	Tutorial	Laboratory	Project	Seminar	SUM
	Number of study hours	30.0	0.0	0.0	0.0	30.0	60
E-learning hours included: 30.0							
Learning activity and number of study hours	Learning activity	Participation in didactic classes included in study plan		Participation in consultation hours		Self-study	SUM
	Number of study hours	60		5.0		35.0	100
Subject objectives	The aim of the lecture is to familiarize students with the basic concepts and facts in the field of dynamical systems and the theory of chaos.						
Learning outcomes	Course outcome	Subject outcome			Method of verification		
	K7_K04	The student understands the importance of fractal geometry and the theory of dynamical systems.			[SK4] Assessment of communication skills, including language correctness		
	K7_U09	The student knows the concepts of dynamical systems and fractal geometry.			[SU1] Assessment of task fulfilment		
	K7_W03	The student knows the Mountain Pass Theorem, the Generalized Ekeland Variational Principle, Sharkovski's Theorem, Kolmogorov's Theorem.			[SW1] Assessment of factual knowledge		
Subject contents	Examples of fractals. Dimensions: fractal dimension, Hausdorff's dimension and topological dimension. The Barnsley and Hutchinson theory. Feigenbaum's bifurcation. Sharkovski's theorem. Hamiltonian systems. The mountain pass theorem. Generalized variational Ekeland principle. Kolmogorov's theorem.						
Prerequisites and co-requisites	Mathematical analysis. Ordinary differential equations. Topology.						
Assessment methods and criteria	Subject passing criteria		Passing threshold		Percentage of the final grade		
	Test		50.0%		50.0%		
	Multimedia presentation		100.0%		50.0%		
Recommended reading	Basic literature		1. Jacek Kudrewicz, Fractals and chaos, WNT, Warsaw, 2007 (in Polish) 2. Jean Mawhin, Michell Willem, Critical Points Theory and Hamiltonian Systems, Springer-Verlag, 1989.				
	Supplementary literature		H.-O. Peitgen, H. Jürgens, D. Saupe, Chaos and Fractals. New Frontiers of Science, Springer, 2004				

	eResources addresses	Podstawowe https://enauczanie.pg.edu.pl/moodle/course/view.php?id=33196 - Adresy na platformie eNauczanie:
Example issues/ example questions/ tasks being completed	<p>1. Please provide the definition of a discrete dynamic system/a continuous dynamical system.2. What is an attractor? Please give examples of strange attractors.3. Please calculate the fractal dimension, Hausdorff's dimension and the topological dimension of given fractals.4. Please list the features of fractals.5. What is the Hamiltonian system?6. Please formulate the Mountain Pass Theorem and give its geometric interpretation.7. What is Sharkovski's theorem about?</p>	
Work placement	Not applicable	