

## Subject card

| Subject name and code                       | Mathematics, PG_00054407                                                                                                                                         |                                                       |                                                                                                                                                                                                                                                                                    |            |        |                                                                    |         |     |  |
|---------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------|--------|--------------------------------------------------------------------|---------|-----|--|
| Field of study                              | Electronics and Telecommunications                                                                                                                               |                                                       |                                                                                                                                                                                                                                                                                    |            |        |                                                                    |         |     |  |
| Date of commencement of studies             | February 2023                                                                                                                                                    |                                                       | Academic year of realisation of subject                                                                                                                                                                                                                                            |            |        | 2022/2023                                                          |         |     |  |
| Education level                             | second-cycle studies                                                                                                                                             |                                                       | Subject group                                                                                                                                                                                                                                                                      |            |        | Obligatory subject group in the field of study                     |         |     |  |
|                                             |                                                                                                                                                                  |                                                       |                                                                                                                                                                                                                                                                                    |            |        | Subject group related to scientific research in the field of study |         |     |  |
| Mode of study                               | Full-time studies                                                                                                                                                |                                                       | Mode of delivery                                                                                                                                                                                                                                                                   |            |        | at the university                                                  |         |     |  |
| Year of study                               | 1                                                                                                                                                                |                                                       | Language of instruction                                                                                                                                                                                                                                                            |            |        | Polish                                                             |         |     |  |
| Semester of study                           | 1                                                                                                                                                                |                                                       | ECTS credits                                                                                                                                                                                                                                                                       |            |        | 6.0                                                                |         |     |  |
| Learning profile                            | general academic profile                                                                                                                                         |                                                       | Assessment form                                                                                                                                                                                                                                                                    |            |        | exam                                                               |         |     |  |
| Conducting unit                             | Mathematics Center -> Vice-Rector for Education                                                                                                                  |                                                       |                                                                                                                                                                                                                                                                                    |            |        |                                                                    |         |     |  |
| Name and surname of lecturer (lecturers)    | Subject supervisor                                                                                                                                               |                                                       | dr Magdalena Musielak                                                                                                                                                                                                                                                              |            |        |                                                                    |         |     |  |
|                                             | Teachers                                                                                                                                                         |                                                       | dr Magdalena Musielak                                                                                                                                                                                                                                                              |            |        |                                                                    |         |     |  |
|                                             |                                                                                                                                                                  |                                                       | dr Hanna Guze                                                                                                                                                                                                                                                                      |            |        |                                                                    |         |     |  |
| Lesson types and methods of instruction     | Lesson type                                                                                                                                                      | Lecture                                               | Tutorial                                                                                                                                                                                                                                                                           | Laboratory | Projec | t                                                                  | Seminar | SUM |  |
|                                             | Number of study hours                                                                                                                                            | 30.0                                                  | 15.0                                                                                                                                                                                                                                                                               | 0.0        | 0.0    |                                                                    | 0.0     | 45  |  |
|                                             | E-learning hours included: 0.0                                                                                                                                   |                                                       |                                                                                                                                                                                                                                                                                    |            |        |                                                                    |         |     |  |
| Learning activity and number of study hours | Learning activity                                                                                                                                                | ning activity Participation in classes including plan |                                                                                                                                                                                                                                                                                    |            |        | Self-study                                                         |         | SUM |  |
|                                             | Number of study hours                                                                                                                                            | 45                                                    | 10.0                                                                                                                                                                                                                                                                               |            | 95.0   |                                                                    | 150     |     |  |
| Subject objectives                          | The use of specialized mathematical tools to technical subjects.                                                                                                 |                                                       |                                                                                                                                                                                                                                                                                    |            |        |                                                                    |         |     |  |
| Learning outcomes                           | Course outcome                                                                                                                                                   |                                                       | Subject outcome                                                                                                                                                                                                                                                                    |            |        | Method of verification                                             |         |     |  |
|                                             | and toolsn                                                                                                                                                       |                                                       | Student uses the notion of linear space, linear transformation, determines matrices of linear transformations in different bases, demonstrates methods for solving differential and integral equations, analyzes stability of linear and nonlinear systems differential equations. |            |        | [SU4] Assessment of ability to use methods and tools               |         |     |  |
|                                             | [K7_W01] Knows and understands, to an increased extent, mathematics to the extent necessary to formulate and solve complex issues related to the field of study. |                                                       | Student knows the basic concepts and theorems of linear algebra, knows the basics of functional analysis, knows the types of differential and integral equations, knows theorems and techniques of solving ordinary differential equations and partial differential equations.     |            |        | [SW1] Assessment of factual knowledge                              |         |     |  |

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| Subject contents                                               | Linear space. Basic concepts. Linear subspace. Basis and dimension of linear space. Coordinates of vector to the base. Linear operators. Basic concepts. Matrix of linear transformation. Change of basis matrix. Hilbert Space. Space L <sup>2</sup> [-,].                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    |                               |  |  |  |  |
|----------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------|--|--|--|--|
|                                                                | First order ordinary differential equations. Basic concepts. Separable equations.Bernoulli equation. Lagrange equation and Clairauta equation. Exact equations. Intergrating factor. Higher order linear equations with constant coefficients. Higher order Euler equations. Second order linear equations with nonconstant coefficients. Systems of differential equations.Qualitative analysis of solutions of ordinary differential equations. Lapunov stability.                                                                                                                                                                                                                                                                                                                                                                                                                                                       |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    |                               |  |  |  |  |
|                                                                | Integral equations. Basic terminology. Classification. Volterra and Fredholm equation. Transforming differential equations into integral equations. Methods for solving integral equations. Successive approximations, iterated kernels, resolvent.  Partial differential equations. Basic concepts. First order partial differential equations. Linear partial differential equations of second order. Methods to solve linear partial differential equations of second order. Classification of equations. Reducing equations to canonical form. Wave equation in one dimensional case. Wave equation. Heat conduction equation. Laplace equation.                                                                                                                                                                                                                                                                       |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    |                               |  |  |  |  |
|                                                                |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    |                               |  |  |  |  |
| Prerequisites and co-requisites                                |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    |                               |  |  |  |  |
| Assessment methods                                             | Subject passing criteria                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | Passing threshold                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | Percentage of the final grade |  |  |  |  |
| and criteria                                                   | Homework assignments                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       | 0.0%                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               | 20.0%                         |  |  |  |  |
|                                                                | Final exam                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 | 50.0%                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              | 80.0%                         |  |  |  |  |
| Recommended reading                                            | Basic literature                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | <ol> <li>Topp, J., Algebra, Wydawnictwo Politechniki Gdańskiej</li> <li>Żakowski, W., Leksiński, W., Podręczniki Akademickie -<br/>Matematyka. Część IV, Wydawnictwo Naukowe PWN</li> <li>Roman, S., Advanced Linear Algebra, Third Edition, Springer</li> <li>Tveito, A., Winther, R., Introduction to Partial Differential<br/>Equations, Springer</li> <li>L. C. Evans, Partial Differential Equations, AMS.</li> <li>Hochstadt, H., Integral Equations, A Wiley-Interscience<br/>Publications</li> <li>M.I.Krasnov, G.I.Makarenko, A.I. Kiselev, Problems and exercises<br/>in the calculus of variations., Mir Publishers.</li> <li>Palczewski, A., Równania różniczkowe zwyczajne, Wydawnictwo<br/>Naukowe PWN</li> <li>Debnath, L., Mikusinski, P., Hilbert Spaces with Applications, Third<br/>Edition, Elsevier Academic Press</li> </ol> |                               |  |  |  |  |
|                                                                | Supplementary literature                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | <ol> <li>Matwiejew, N. M., Zadania z równań różniczkowych zwyczajnych,<br/>Wydawnictwo Naukowe PWN</li> <li>Krasnow, M. L., Kisielew, A. I., Makarenko, G. I., Zadania z równań<br/>całkowych, Wydawnictwo Naukowe PWN</li> <li>Rutkowski, J., Algebra abstrakcyjna w zadaniach, Wydawnictwo<br/>Naukowe PWN</li> </ol>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            |                               |  |  |  |  |
|                                                                | eResources addresses                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       | Adresy na platformie eNauczanie: WETI - EiT II stopien - Matematyka 2022/23 (M.Musielak) - Moodle ID: 28935 https://enauczanie.pg.edu.pl/moodle/course/view.php?id=28935                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           |                               |  |  |  |  |
| Example issues/<br>example questions/<br>tasks being completed | <ol> <li>Verify if the given transformation T: R<sub>2x2</sub>R<sub>2</sub>[x] is linear. In case of positive answer find ker T, im T, dim ker T, dim im T. T ([a b; c d])= ax²+(b-c)x +d (R<sub>2x2</sub>,+,·) vector space of real matrices of order 2, with addition and scalar multiplications, (R<sub>2</sub>[x],+,·) vector space of real polynomials of order at most 2, with addition and scalar multiplications.)</li> <li>Solve the following nonhomogeneous linear equation. y"'+y"=(x-1)/(x²).</li> <li>Examine stability of equilibrium points of the system {x'=xy+2y^2; y'=(y-1)(x+2)}</li> <li>Find the integral surface passing through given curve (u)/(x) + y (u)/(y)=u²y, y=t, y=t², u=1.</li> <li>Classify the equation and find its characteristics (²u)/(x²) - 2 cos x (²u)/(x y) -(3 +sin² x) (²u)/(1 y²) -y (u)/(y)=0.</li> <li>Find the resolvent kernel, if K(x,t)=x² t²; a=-1, b=1.</li> </ol> |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    |                               |  |  |  |  |
| Work placement                                                 | Not applicable                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    |                               |  |  |  |  |

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