



## Subject card

|   |   |  |  |                                     |  |            |     |
|---|---|--|--|-------------------------------------|--|------------|-----|
| Subject name and code                       | Linear algebra, PG_00021020   |  |  |                                     |  |            |     |
| Field of study                              | Mathematics   |  |  |                                     |  |            |     |
| Date of commencement of studies             | October 2023  |  | Academic year of realisation of subject                                |                                     | 2023/2024  |            |     |
| Education level                             | first-cycle studies   |  | Subject group  |                                     | Obligatory subject group in the field of study<br>Subject group related to scientific research in the field of study |            |     |
| Mode of study                               | Full-time studies   |  | Mode of delivery   |                                     | at the university  |            |     |
| Year of study                               | 1   |  | Language of instruction  |                                     | Polish   |            |     |
| Semester of study                           | 1   |  | ECTS credits   |                                     | 5.0  |            |     |
| Learning profile                            | general academic profile  |  | Assessment form  |                                     | assessment   |            |     |
| Conducting unit                             | Department of Nonlinear Analysis and Statistics -> Faculty of Applied Physics and Mathematics |  |  |                                     |  |            |     |
| Name and surname of lecturer (lecturers)    | Subject supervisor  |  | dr Joanna Cyman  |                                     |  |            |     |
|   | Teachers  |  | dr Joanna Cyman  |                                     |  |            |     |
|   |   |  | mgr inż. Tomasz Gzella   |                                     |  |            |     |
| Lesson types and methods of instruction     | Lesson type   | Lecture  | Tutorial   | Laboratory                          | Project  | Seminar    | SUM |
|   | Number of study hours   | 30.0   | 30.0   | 0.0                                 | 0.0  | 0.0        | 60  |
|   | E-learning hours included: 0.0  |  |  |                                     |  |            |     |
| Learning activity and number of study hours | Learning activity   | Participation in didactic classes included in study plan |  | Participation in consultation hours |  | Self-study | SUM |
|   | Number of study hours   | 60   |  | 5.0                                 |  | 60.0       | 125 |
| Subject objectives                          | Basic notions of linear algebra   |  |  |                                     |  |            |     |
| Learning outcomes                           | Course outcome  |  | Subject outcome  |                                     | Method of verification   |            |     |
|   | K6_U01  |  | proving simple properties of matrices, linear independence of vectors, |                                     | [SU2] Assessment of ability to analyse information<br>[SU4] Assessment of ability to use methods and tools           |            |     |
|   | K6_W07  |  | linear properties in calculus and other parts of mathematics           |                                     | [SW1] Assessment of factual knowledge  |            |     |
|   | K6_U08  |  | complex numbers, determinants, matrices,                               |                                     | [SU4] Assessment of ability to use methods and tools   |            |     |
|   | K6_W04  |  | formulates theorems and definitions                                    |                                     | [SW1] Assessment of factual knowledge  |            |     |
|   | K6_U03  |  | proper use of algebraic objects  |                                     | [SU3] Assessment of ability to use knowledge gained from the subject   |            |     |

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|--|--|---|-------------------------------|
| Subject contents   | Complex numbers. Operations on complex numbers. Solving algebraic equations in the complex domain. Different forms of a complex number. Geometric interpretation, Gaussian plane. powers of numbers, n-th root. The field of complex numbers. Complex polynomials. Fundamental theorem of algebra. |   |                               |
|  | Matrix calculus. Operations on matrices. Determinants. Laplace expansion. Inverse matrix. Matrix order, elementary matrix transformations.   |   |                               |
|  | Systems of linear equations. Cramer's system of equations. The existence of solutions to a system of linear equations, the Kronecker-Capelli theorem. Gauss Jordan method.   |   |                               |
|  | Basic algebraic structures. Groups, rings, bodies. Definitions and examples.   |   |                               |
|  | Vector space. Definition of vector space and subspace. Testing the linear independence of vectors.   |   |                               |
| Prerequisites and co-requisites                                |  |   |                               |
| Assessment methods and criteria                                | Subject passing criteria   | Passing threshold   | Percentage of the final grade |
|  | 2 written tests  | 50.0%   | 80.0%                         |
|  | activity   | 30.0%   | 20.0%                         |
| Recommended reading  | Basic literature   | Jurlewicz, Z. Skoczylas, Linear Algebra 1 i 2. Definitions, theorems, formulas, Oficyna Wydawnicza GiS, Wrocław 2012.   |                               |
|  |  | T. Jurlewicz, Z. Skoczylas, Linear Algebra 1 i 2. Examples and tasks, Oficyna Wydawnicza GiS, Wrocław 2012.   |                               |
|  |  | J. Topp, Linear Algebra, Wydawnictwo Uniwersytetu Gdańskiego, Gdańsk 2015.  |                               |
|  | Supplementary literature   | J. Rutkowski, Linear Algebra liniowa in problems, PWN 2008  |                               |
|  |  | G. Banaszak, W. Gajda, Elements of linear algebraj, WNT 2002.   |                               |
|  |  | A. Romanowski, Linear Algebra, Wyd. PG 2003.  |                               |
|  | eResources addresses   | Adresy na platformie eNauczanie:<br>Algebra liniowa 2023/2024 - Moodle ID: 33214<br><a href="https://enauczanie.pg.edu.pl/moodle/course/view.php?id=33214">https://enauczanie.pg.edu.pl/moodle/course/view.php?id=33214</a> |                               |
| Example issues/<br>example questions/<br>tasks being completed | 1. Draw the set $2< (3+4i)z+i <3$  |   |                               |
|  | 2. Solve the given system of equations:  |   |                               |
|  | 4x+y+3z-t=5<br>2x-y+3z+2t=2<br>3x+y+2z-t=1<br>5x+y+4z+2t=0   |   |                               |
|  | 3. Define the vector space.  |   |                               |
| Work placement   | Not applicable   |   |                               |