



Subject card

Subject name and code	Topology, PG_00021501						
Field of study	Mathematics						
Date of commencement of studies	October 2023	Academic year of realisation of subject			2024/2025		
Education level	first-cycle studies	Subject group			Obligatory subject group in the field of study Subject group related to scientific research in the field of study		
Mode of study	Full-time studies	Mode of delivery			at the university		
Year of study	2	Language of instruction			Polish		
Semester of study	3	ECTS credits			5.0		
Learning profile	general academic profile	Assessment form			exam		
Conducting unit	Institute of Applied Mathematics -> Faculty of Applied Physics and Mathematics						
Name and surname of lecturer (lecturers)	Subject supervisor	dr hab. Zdzisław Dzedzej					
	Teachers	dr inż. Maciej Starostka dr hab. Zdzisław Dzedzej					
Lesson types and methods of instruction	Lesson type	Lecture	Tutorial	Laboratory	Project	Seminar	SUM
	Number of study hours	30.0	30.0	0.0	0.0	0.0	60
	E-learning hours included: 0.0						
	Adresy na platformie eNauczanie: Topologia 24-25 - Moodle ID: 39856 https://enauczanie.pg.edu.pl/moodle/course/view.php?id=39856						
Learning activity and number of study hours	Learning activity	Participation in didactic classes included in study plan	Participation in consultation hours	Self-study	SUM		
	Number of study hours	60	5.0	60.0	125		
Subject objectives	Introduction to topology of metric spaces, intuitions and proof techniques.						
Learning outcomes	Course outcome	Subject outcome			Method of verification		
	K6_U02	The student is able to prove elementary topological theorems.			[SU1] Assessment of task fulfilment		
	K6_W07	The student knows the basic concepts and theorems of topology.			[SW1] Assessment of factual knowledge		
	K6_U09	The student is able to examine the properties of sets under different metrics.			[SU4] Assessment of ability to use methods and tools [SU2] Assessment of ability to analyse information		
	K6_U03	The student knows how to use topological concepts in mathematical analysis.			[SU4] Assessment of ability to use methods and tools [SU1] Assessment of task fulfilment		
K6_W04	The student knows the basic concepts and theorems of topology.			[SW1] Assessment of factual knowledge			

Subject contents	Lectures: Metric spaces: metrics and metric space, examples. Notion of an open ball in metric space. Closed set. Cartesian product of metric spaces, Hilbert space. Topological spaces: topological space, examples. Interior, closure and boundary of a set in topological space. Dense subsets, dense countable subsets, separable spaces. Continuity and homeomorphisms: Continuity of a map in topological spaces. Equivalence of Heine and Cauchy conditions and continuity in metric spaces. Homeomorphism and homeomorphic spaces. Uniformly continuous maps and Lipschitz functions in metric spaces. Complete metric spaces: Cauchy sequences and complete metric spaces. Banach space. Cantor's theorem and Banach theorem with applications. Theorem on embedding of metric spaces in complete metric spaces. Compactness: Compact sets and their characterizations. Properties of continuous maps on compact sets. Cantor set and its properties, examples of non-typical continuous functions constructed by use of this set. Tichonov theorem. Hilbert cube. Boundary sets and nowhere dense sets, Baire theorem. Connectedness: Connected spaces and their properties. The interval $[0,1]$ is connected. Properties of continuous maps on connected sets. Closure and cartesian product of connected spaces. Path connected and locally path connected spaces. Warsaw circle and harmonic fan. Exercises: Examples and notions from lectures will be discussed, elementary theorems will be proved, geometric problems will be solved.		
Prerequisites and co-requisites	Knowledge of some notions from mathematical analysis and set theory.		
Assessment methods and criteria	Subject passing criteria	Passing threshold	Percentage of the final grade
	written exam	50.0%	50.0%
	Midterm colloquium	50.0%	40.0%
	activity	0.0%	10.0%
Recommended reading	Basic literature	1. H. Patkowska, Wstęp do topologii, PWN, Warszawa-Poznań, 2000. 2. K. Kuratowski, Wstęp do teorii mnogości i topologii, PWN, Warszawa, 1972. 3. R. Duda, Wprowadzenie do topologii I/II, PWN, Warszawa, 1986.	
	Supplementary literature	K. Sieklucki, Geometria i Topologia cz. I, Geometria, PWN, Warszawa 1978. K. Sieklucki i R. Engelking, Geometria i Topologia cz. II, Topologia, PWN, Warszawa 1980.	
	eResources addresses	Topologia 24-25 - Moodle ID: 39856 https://enauczenie.pg.edu.pl/moodle/course/view.php?id=39856	
Example issues/ example questions/ tasks being completed	Investigate properties of the set $\{(x,y): \sqrt{(x-1)^2+(y-1)^2} \leq 1\}$ with various metrics		
Work placement	Not applicable		

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