



Subject card

Subject name and code	Introduction to stochastic modeling, PG_00025513						
Field of study	Mathematics						
Date of commencement of studies	October 2023		Academic year of realisation of subject		2025/2026		
Education level	first-cycle studies		Subject group		Optional subject group Subject group related to scientific research in the field of study		
Mode of study	Full-time studies		Mode of delivery		blended-learning		
Year of study	3		Language of instruction		Polish		
Semester of study	5		ECTS credits		4.0		
Learning profile	general academic profile		Assessment form		exam		
Conducting unit	Department of Probability Theory and Biomathematics -> Faculty of Applied Physics and Mathematics						
Name and surname of lecturer (lecturers)	Subject supervisor		dr inż. Anna Szafrńska				
	Teachers						
Lesson types and methods of instruction	Lesson type	Lecture	Tutorial	Laboratory	Project	Seminar	SUM
	Number of study hours	30.0	15.0	0.0	15.0	0.0	60
	E-learning hours included: 8.0						
	Adresy na platformie eNauczanie:						
Learning activity and number of study hours	Learning activity	Participation in didactic classes included in study plan		Participation in consultation hours		Self-study	SUM
	Number of study hours	60		5.0		35.0	100
Subject objectives	Introduction to modelling of random events and their simulations in R.						
Learning outcomes	Course outcome		Subject outcome		Method of verification		
	K6_U07		Student analyzes models of random phenomena occurring in biology and medicine.		[SU3] Assessment of ability to use knowledge gained from the subject [SU4] Assessment of ability to use methods and tools		
	K6_U10		Student studies asymptotic properties of trajectories of discrete dynamical systems. Designs random numbers generators with a given distribution. Simulates Markov chains.		[SU1] Assessment of task fulfilment [SU3] Assessment of ability to use knowledge gained from the subject [SU4] Assessment of ability to use methods and tools		
	K6_K02		Student simulates and analyzes random phenomena occurring in biology and medicine.		[SK2] Assessment of progress of work [SK5] Assessment of ability to solve problems that arise in practice		
	K6_W09		Student programs in the R package.		[SW3] Assessment of knowledge contained in written work and projects		
	K6_U11		Student designs and simulates random numbers generators with a given distribution. Student simulates Markov chains.		[SU1] Assessment of task fulfilment [SU3] Assessment of ability to use knowledge gained from the subject		

Subject contents	LECTURES General notions of mathematical modeling. Random and deterministic events in technology, physic, biology and socio-economic life. Deterministic dynamical systems. Deterministic chaos. Random variables. Pseudo random numbers and their generators. Random walks and their simulations. Markov chains and their simulations. Birth and death processes. Monte Carlo methods.		
	TUTORIALS Analysis of asymptotic properties of trajectories of discrete time dynamical systems. Generating pseudo random numbers with given distributions. Algebraic methods of iterating of stochastic matrices,. Recurrence of random walks. Expected time of the first return for n-dimensional random walks. Stationary distributions.		
	PROJECTS Computer supported analysis of asymptotic properties of trajectories of discrete time dynamical systems. Generating of pseudo-random sequences of a given distribution. Simulation of random walks and Markov chains.		
Prerequisites and co-requisites	Courses completed: Probability Theory term IV (MAT1013/1), Mathematical Analysis (MAT1001)		
Assessment methods and criteria	Subject passing criteria	Passing threshold	Percentage of the final grade
	Test 1, 2	50.0%	20.0%
	Research project 2	50.0%	20.0%
	Research project 1	50.0%	10.0%
	Exam	50.0%	50.0%
Recommended reading	Basic literature	1. P. Biecek, Przewodnik po pakiecie R, GiS, Wrocław, 2014. 2. R. Wieczorkowski, R. Zieliński, Komputerowe generatory liczb losowych, WNT, Warszawa, 1997. 3. R. Snopkowski, Symulacja stochastyczna, AGH, Kraków, 2007. 4. Urszula Foryś, Matematyka w Biologii, WNT Warszawa 2005.	
	Supplementary literature	1. M. Gagolewski, Programowanie w języku R, Wydawnictwo Naukowe PWN, 2014. 2. A. Janicki, A. Izydorczyk, Komputerowe metody w modelowaniu stochastycznym, WNT, Warszawa, 2001. 3. L. Smith, Chaos, Oxford University Press, Oxford, 2007. 4. D.E.Knuth, The Art of Computer Programming, Addison-Wesley, New York, 1997. 5. J. Jakubowski, R. Sztencel, Wstęp do teorii prawdopodobieństwa, Script, Warszawa, 2001. 6. J.Haigh, Probability Models, Springer, 2013.	
	eResources addresses		
Example issues/ example questions/ tasks being completed	Analyse asymptotic properties of trajectories of discrete time dynamical systems. Generate pseudo-random sequences of a given distribution. Simulate Markov chain.		
Work placement	Not applicable		