



Subject card

Subject name and code	Linear algebra and geometry, PG_00061892						
Field of study	Materials Engineering						
Date of commencement of studies	October 2023	Academic year of realisation of subject			2023/2024		
Education level	first-cycle studies	Subject group			Obligatory subject group in the field of study		
Mode of study	Full-time studies	Mode of delivery			at the university		
Year of study	1	Language of instruction			Polish		
Semester of study	1	ECTS credits			4.0		
Learning profile	general academic profile	Assessment form			assessment		
Conducting unit	Mathematics Center -> Vice-Rector for Education						
Name and surname of lecturer (lecturers)	Subject supervisor	dr Anna Niewulis					
	Teachers	dr Anna Niewulis mgr Justyna Woron					
Lesson types and methods of instruction	Lesson type	Lecture	Tutorial	Laboratory	Project	Seminar	SUM
	Number of study hours	15.0	30.0	0.0	0.0	0.0	45
	E-learning hours included: 0.0						
Learning activity and number of study hours	Learning activity	Participation in didactic classes included in study plan	Participation in consultation hours		Self-study	SUM	
	Number of study hours	45	5.0		50.0	100	
Subject objectives	The aim of this subject is to obtain the students competence in the range of using the basic methods of algebra. Furthermore, the student is able to use this knowledge to solve simple theoretical and practical problems that can be found in the field of engineering.						
Learning outcomes	Course outcome	Subject outcome			Method of verification		
	[K6_U05] can learn independently	Student recognizes the importance of self-expanding knowledge.			[SU3] Assessment of ability to use knowledge gained from the subject [SU2] Assessment of ability to analyse information		
	[K6_K01] Understands the need to improve professional and personal competencies; is conscious of own limitations and knows when to turn to experts, properly establishes priorities helping to accomplish tasks defined by oneself or others.	Student combines knowledge of mathematics with knowledge from other fields.			[SK5] Assessment of ability to solve problems that arise in practice [SK4] Assessment of communication skills, including language correctness		
	[K6_W01] Has knowledge of selected branches of mathematics, useful for formulating and solving problems and describing mechanical and physical phenomena, and chemical processes.	Student uses methods of mathematical description of phenomena in the physical / mechanical / chemical processes.			[SW3] Assessment of knowledge contained in written work and projects [SW2] Assessment of knowledge contained in presentation		

Subject contents	<p>Elements of linear algebra: Matrices (definition, types of matrices, matrix operations). Determinants and their properties. Rank of a matrix. Matrices, their properties and operations on matrices. Inverse of a square non-singular matrix.</p> <p>Systems of linear equations : Systems of linear equations. Cramers theorem. Rank of matrix. Kronecker-Capelly theorem.</p> <p>Analytic geometry: Basic vectors definitions and properties. Eigenvectors and eigenvalues. Dot product, cross product, their properties and its applications. The triple scalar product and applications. Equations of lines and planes in 3-space. The distance from a point to a plan. Angles between planes and lines.</p> <p>Complex numbers. Algebraic, trigonometric, exponential form, operations, exponentiation (Moivre formula), finding roots of complex numbers. Operations on complex numbers.</p>								
Prerequisites and co-requisites									
Assessment methods and criteria	<table border="1" data-bbox="448 920 1477 985"> <thead> <tr> <th data-bbox="448 920 794 954">Subject passing criteria</th> <th data-bbox="794 920 1141 954">Passing threshold</th> <th data-bbox="1141 920 1477 954">Percentage of the final grade</th> </tr> </thead> <tbody> <tr> <td data-bbox="448 954 794 985">Colloquium</td> <td data-bbox="794 954 1141 985">50.0%</td> <td data-bbox="1141 954 1477 985">100.0%</td> </tr> </tbody> </table>			Subject passing criteria	Passing threshold	Percentage of the final grade	Colloquium	50.0%	100.0%
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Colloquium	50.0%	100.0%							
Recommended reading	Basic literature	<ol style="list-style-type: none"> 1. Gewert M., Skoczylas Z., Algebra liniowa 1, Definicje, twierdzenia wzory, Wydawnictwo GiS, Wrocław 2. Gewert M., Skoczylas Z., Algebra liniowa 2, Definicje, twierdzenia wzory, Wydawnictwo GiS, Wrocław 3. K. Jankowska, T. Jankowski, Zbiór zadań z matematyki, PG Gdańsk 4. Banaś J., Podstawy matematyki dla ekonomistów, Wydawnictwa Naukowo-Techniczne, Warszawa 5. Matłoka M., Wojcieszyn B., Matematyka z elementami zastosowań w ekonomii, Wydawnictwo Wyższej Szkoły Bankowej w Poznaniu 							
	Supplementary literature	<ol style="list-style-type: none"> 1. K. Jankowska, T. Jankowski "Zbiór zadań z matematyki wyższej", Wyd. PG, Gdańsk 1999, 2. B. Gdowski, E. Pluciński "Zadania z rachunku wektorowego i geometrii analitycznej", PWN, Warszawa 1982 3. I. Dziubiński, L. Siewierski Matematyka dla wyższych szkół technicznych , PWN, Warszawa 1984, 							
	eResources addresses	Adresy na platformie eNauzanie: FTiMS_IM - Algebra liniowa z geometrią - 2023/2024 (A.Niewulis) - Moodle ID: 23992 https://enauzanie.pg.edu.pl/moodle/course/view.php?id=23992 FTiMS_IM - Algebra liniowa z geometrią - 2023/2024 (A.Niewulis) - Moodle ID: 23992 https://enauzanie.pg.edu.pl/moodle/course/view.php?id=23992							

Example issues/ example questions/ tasks being completed	1. Find an equation for the plane satisfying the given conditions: a) passes through the z-axis and the point P , b) passes through the point P and is perpendicular to the line l . 2. Discuss the relation between the line l and the plane S . 3. Find the rank of the matrix A .
Work placement	Not applicable