



Subject card

Subject name and code	Multibody systems, PG_00057034						
Field of study	Mechatronics						
Date of commencement of studies	February 2024	Academic year of realisation of subject			2024/2025		
Education level	second-cycle studies	Subject group			Obligatory subject group in the field of study Subject group related to scientific research in the field of study		
Mode of study	Full-time studies	Mode of delivery			at the university		
Year of study	1	Language of instruction			Polish None		
Semester of study	2	ECTS credits			2.0		
Learning profile	general academic profile	Assessment form			exam		
Conducting unit	Zakład Mechaniki Stosowanej i Biomechaniki -> Institute of Mechanics and Machine Design -> Faculty of Mechanical Engineering and Ship Technology						
Name and surname of lecturer (lecturers)	Subject supervisor	dr hab. inż. Krzysztof Lipiński					
	Teachers						
Lesson types and methods of instruction	Lesson type	Lecture	Tutorial	Laboratory	Project	Seminar	SUM
	Number of study hours	15.0	0.0	0.0	15.0	0.0	30
	E-learning hours included: 0.0						
Learning activity and number of study hours	Learning activity	Participation in didactic classes included in study plan	Participation in consultation hours	Self-study	SUM		
	Number of study hours	30	4.0	16.0	50		
Subject objectives	Students are familiarized with some methods of determination of the position; orientation; velocity and acceleration of a body in space. Students are familiarized with the idea of system description in absolute, normal and joint coordinates. Formulation and solution of constrain equations for closed kinematic chains. Students are familiarized with the main aspects and equations of open kinematic chains dynamics and of closed kinematical chains, using the Lagrange equations .						
Learning outcomes	Course outcome	Subject outcome			Method of verification		
	[K7_W03] has detailed, supported by the theory knowledge in terms of analytical mechanics, theory of mechanisms and machine dynamics, multibody systems, micromechanisms and microdrives	has theoretically founded detailed knowledge in the field of analytical mechanics, theory of mechanisms and dynamics of machines, multibody systems,			[SW1] Assessment of factual knowledge		
	[K7_U04] is able to utilise known methods and mathematical models, as well as computer simulations for analysis and evaluation of non-stationary continuous and discrete mechatronic systems and processes	can use the known methods and mathematical models, as well as computer simulations to analyze and evaluate dynamics of mechanical and mechatronic systems			[SU1] Assessment of task fulfilment		
	[K7_U05] is able to formulate and test hypothesis concerning problems of nonstationary systems and processes and simple research problems	is able to formulate and test hypotheses related to the problems of dynamics of systems of many solids connected by constraints			[SU4] Assessment of ability to use methods and tools		

Subject contents	The students are familiarized with some methods of determination of the position and orientation of a body in space, presentation of a vector as a matrix product of a column matrix (a vector) of coordinates and a table of unit vectors, he is familiarized with use of the orientation matrices, how calculate the products of the matrices and the column matrix of coordinates of a vector, and how to formulate the elements of the orientation matrices as a functions of the system coordinates. The students are familiarized with the idea of system description in absolute, normal and joint coordinates. Presentation of description methods useful in description of the system topology. Formulation and solution of constrain equations for closed kinematic chains. Presentation of the selection methods useful in dependent coordinates selection. Presentation of the relationship arising from the derivation of the constrain equations, constrain equations at level of speeds and accelerations of the multibody system coordinates. Presentation of methods used to determine the dynamics equations of a particle and of a rigid body. Presentation of methods used to transform the dynamics equations between the selected types of system coordinates. The students are familiarized with the main aspects and equations of open kinematic chains dynamics and of closed kinematical chains, using the Lagrange equations of the second kind, using the Lagrange equations of the first kind and the elimination of dependent coordinates. The students are familiarized with the methods of eliminating of violations of the constraints equations. Presentation of example descriptions and analyzes of dynamics time variable configurations of the multibody systems.											
Prerequisites and co-requisites	Passed courses in subjects Matematyka, Mechanika I, Mechanika II, Theory of mechanisms and machines (or Kinematics and Dynamics of Machines)											
Assessment methods and criteria	<table border="1" data-bbox="448 546 1498 651"> <thead> <tr> <th data-bbox="448 546 794 584">Subject passing criteria</th> <th data-bbox="794 546 1141 584">Passing threshold</th> <th data-bbox="1141 546 1498 584">Percentage of the final grade</th> </tr> </thead> <tbody> <tr> <td data-bbox="448 584 794 618">project grade - an obligatory part</td> <td data-bbox="794 584 1141 618">56.0%</td> <td data-bbox="1141 584 1498 618">50.0%</td> </tr> <tr> <td data-bbox="448 618 794 651">written exam - an obligatory part</td> <td data-bbox="794 618 1141 651">56.0%</td> <td data-bbox="1141 618 1498 651">50.0%</td> </tr> </tbody> </table>			Subject passing criteria	Passing threshold	Percentage of the final grade	project grade - an obligatory part	56.0%	50.0%	written exam - an obligatory part	56.0%	50.0%
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Example issues/ example questions/ tasks being completed	<p>1. Reasons of non-linearity of models of multibody systems 2. Differences between a multibody system with an open structure and a closed structure 3. Description in independent coordinates - advantages and disadvantages 4. Description in dependent coordinates - advantages and disadvantages 5. Description in absolute coordinates - advantages and disadvantages 6. Description in joint coordinates - advantages and disadvantages 7. Description in natural coordinates - advantages and disadvantages 8. Constraint equations and their applications in the dynamics of multibody systems 9. constraints for position, velocity and acceleration, Jacobian of the constraint equations 10. Gauss elimination algorithm and passive constraints 11. The Newton-Raphson algorithm for solving a system of nonlinear equations 12. Lagrange equations of I kind (Lagrange multipliers technique) 13. Elimination of multipliers and dependent coordinates 14. The orientation matrix in dynamics of the spatial (3D) multibody systems 15. Euler angles / Cardan angles / Euler parameters 16. The derivatives of the orientation matrix and angular velocity 17. Transformations of dynamics equations to alternative coordinates 18. Equations of kinematics and dynamics of the open kinematic chain</p>											
Work placement	Not applicable											