



Subject card

Subject name and code	Mathematics III, PG_00059248						
Field of study	Matematyka III						
Date of commencement of studies	October 2024	Academic year of realisation of subject			2025/2026		
Education level	first-cycle studies	Subject group			Obligatory subject group in the field of study		
Mode of study	Full-time studies	Mode of delivery			at the university		
Year of study	2	Language of instruction			Polish		
Semester of study	3	ECTS credits			5.0		
Learning profile	general academic profile	Assessment form			exam		
Conducting unit	Mathematics Center -> Vice-Rector For Education						
Name and surname of lecturer (lecturers)	Subject supervisor	dr inż. Renata Zakrzewska					
	Teachers	mgr Katarzyna Kiepiela dr inż. Renata Zakrzewska mgr Małgorzata Kula mgr Danuta Beger					
Lesson types	Lesson type	Lecture	Tutorial	Laboratory	Project	Seminar	SUM
	Number of study hours	30.0	30.0	0.0	0.0	0.0	60
	E-learning hours included: 0.0						
	eNauczanie source addresses: Moodle ID: 46676 WLiŚ - Bud. sem 3 - Matematyka 2025/2026 (R.Zakrzewska) https://enauczanie.pg.edu.pl/moodle/course/view.php?id=46676						
Learning activity and number of study hours	Learning activity	Participation in didactic classes included in study plan	Participation in consultation hours	Self-study	SUM		
	Number of study hours	60	5.0	60.0	125		
Subject objectives	Students obtain competence in the range of using methods of mathematical analysis and linear algebra and knowledge how to solve simple problems that can be found in the field of engineering.						

Learning outcomes	Course outcome	Subject outcome	Method of verification
	[K6_U01] Apply knowledge and understanding of mathematics as well as sciences and engineering disciplines underlying civil engineering to solve engineering problems and issues.	Student compute multiple integrals and use them in geometry and mechanics. Student gives definition of notions from field theory. Student studies convergence of number series. Student uses power series in order to compute sums of number series. Student calculates the probability of random events. Student describes the basic types of distributions of random variables. Student compute multiple integrals and use them in geometry and mechanics. Student gives definition of notions from field theory. Student studies convergence of number series. Student uses power series in order to compute sums of number series. Student calculates the probability of random events. Student describes the basic types of distributions of random variables.	[SU1] Ocena realizacji zadania
	[K6_W01] Demonstrate knowledge and understanding of mathematics as well as sciences and engineering disciplines underlying civil engineering at a level necessary to achieve the other programme outcomes.	Student compute multiple integrals and use them in geometry and mechanics. Student gives definition of notions from field theory. Student studies convergence of number series. Student uses power series in order to compute sums of number series. Student calculates the probability of random events. Student describes the basic types of distributions of random variables.	[SW1] Ocena wiedzy faktograficznej
Subject contents	<p>Double and triple integrals. Applications of multiple integrals. Elements of field theory: Scalar and vector fields, the gradient of a scalar field,</p> <p>divergence and rotation of a vector field, a potential field. Line integrals with applications.</p> <p>Number series and function series: Number series. Convergent and divergent series. Convergence tests of the number series. Power series. Radius and interval of convergence. Calculus of probability: Discrete and continuous random variables, distribution function, expected value and variance of a random variable. Basic distribution of random variables.</p>		
Prerequisites and co-requisites			
Assessment methods and criteria	Subject passing criteria	Passing threshold	Percentage of the final grade
	midterm colloquium	50.0%	60.0%
	written exam	50.0%	40.0%

Recommended reading	Basic literature	<p>J. Dymkowska, D. Beger, Rachunek całkowity w zadaniach, PG, Gdańsk 2015</p> <p>K. Jankowska, T. Jankowski, Zadania z matematyki wyższej, PG, Gdańsk 1999 K. Jankowska, T. Jankowski, Funkcje wielu zmiennych, całki wielokrotne, geometria analityczna, PG, Gdańsk 2005. W. Krysicki, Rachunek prawdopodobieństwa i statystyka matematyczna w zadaniach I, Wydawnictwo Naukowe PWN, Warszawa 2005 A Plucińska, E. Pluciński, Elementy probablistyki, Wydawnictwo Naukowe PWN, Warszawa 1981 W. Stankiewicz, Zadania z matematyki dla wyższych uczelni technicznych, Wydawnictwo Naukowe PWN, Warszawa 1995</p>
	Supplementary literature	<p>M. Gewert, Z. Skoczylas, Elementy analizy wektorowej, Oficyna Wydawnicza GiS, Wrocław 2003 R. Leitner, J. Zacharski, Zarys matematyki wyższej II, Wydawnictwa Naukowo-Techniczne, Warszawa 2005. R. Leitner, J. Zacharski, Zarys matematyki wyższej III, Wydawnictwa Naukowo-Techniczne, Warszawa 2005. R. Leitner, W. Matuszewski, Z. Rojek, Zadania z matematyki wyższej II, Wydawnictwa Naukowo-Techniczne, Warszawa 1999. W. Krysicki, L. Włodarski Analiza matematyczna w zadaniach II, Wydawnictwo Naukowe PWN, Warszawa 1998. B. Gdowski, Elementy geometrii różniczkowej w zadaniach, Wydawnictwo Naukowe PWN, Warszawa 1982 . W. Żakowski, M. Kołodziej, Matematyka - część III, Wydawnictwa Naukowo-Techniczne, Warszawa 1963.</p>
	eResources addresses	

<p>Example issues/ example questions/ tasks being completed</p>	<ol style="list-style-type: none"> 1. Find a potential field for $F(x,y,z)=[2x+yz, 2y+xz, 2z+xy]$. 2. Calculate line integral $\int_L x \, dl$, $L: y=x, 0 \leq x \leq 1$ 3. Check whether the given series is convergent with general term $a_n=1/n \operatorname{tg}(1/n^3)$, $b_n=n!/n^n$, $c_n=1/n \ln n$, using the ratio test, the root test, the comparison test or the integral test. 4. Give the probability distribution and cumulative distribution function for the given discrete random variable X: $x_1=-1, p_1=0,4, x_2=2, p_2=0,6$. 5. Compute the expectation and variation of the given continuous random variable $f(x)=2x$ dla $0 \leq x \leq 2$ i $f(x)=0$ dla $x < 0, x > 2$. 6. Find the area between the two curves $y^2=4+x$ and $x+3y=0$. 7. Using cylindrical or spherical coordinates evaluate the triple integral of the given function $f(x,y,z)=x^2+y^2+z^2$ over the region $V: x^2+y^2+z^2=4, z \geq \sqrt{x^2+y^2}$.
<p>Practical activities within the subject</p>	<p>Not applicable</p>

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