



Subject card

Subject name and code	Stochastic integral, PG_00021509						
Field of study	Mathematics						
Date of commencement of studies	October 2024	Academic year of realisation of subject			2024/2025		
Education level	second-cycle studies	Subject group					
Mode of study	Full-time studies	Mode of delivery			at the university		
Year of study	1	Language of instruction			Polish		
Semester of study	2	ECTS credits			5.0		
Learning profile	general academic profile	Assessment form			exam		
Conducting unit	Department of Nonlinear Analysis and Statistics -> Faculty of Applied Physics and Mathematics						
Name and surname of lecturer (lecturers)	Subject supervisor	prof. dr hab. inż. Tomasz Szarek					
	Teachers	prof. dr hab. inż. Tomasz Szarek Gabriela Łuczyńska					
Lesson types and methods of instruction	Lesson type	Lecture	Tutorial	Laboratory	Project	Seminar	SUM
	Number of study hours	30.0	30.0	0.0	0.0	0.0	60
	E-learning hours included: 0.0						
Learning activity and number of study hours	Learning activity	Participation in didactic classes included in study plan		Participation in consultation hours		Self-study	SUM
	Number of study hours	60		5.0		60.0	125
Subject objectives	Main aim is to equip the student is advanced mathematical tools in technical subjects.						
Learning outcomes	Course outcome		Subject outcome		Method of verification		
Subject contents	Probability spaces with filtration. Stochastic basis. Stopping times and their basic properties. Classification of stopping times. Optional i prognose sigam-algebras. Increasing processes, processes with finite variation and processes with integrable variation. Localization. martingales with continuous time. and their basic properties. The Doob-Meyer decomposition. Square integrable martingales. Stochastic integral with respect to local martingales with continuous paths. and their basic properties. Ito's formula and its applications.. The Girsanov theorem. The decomposition of local martingales. Stochastic integral with respect to local martingales and semimartingales.						
Prerequisites and co-requisites	Probability theory, measure theory and functional analysis.						
Assessment methods and criteria	Subject passing criteria		Passing threshold		Percentage of the final grade		
	Colloquium 1		51.0%		20.0%		
	Exam		51.0%		60.0%		
	Colloquium 2		51.0%		20.0%		
Recommended reading	Basic literature		1) R. Elliot: Stochastic calculus and applications, Springer 1982. 2) H. Kuo, Introduction to stochastic integration, Springer 2006.				

	Supplementary literature	<p>1) C. Dillecherie, P..A. Meyer, Probabilities and potential, tom 2., North-Holland 1982..</p> <p>2) P. Protter, Stochastic Integration and differential equations, Springer 1990.</p> <p>3) O. Kallenberg, Foundations of modern probability, Springer 2001.</p> <p>4) Sheng-wu He, Jia-gang Wang, Jia-an Yan, Semimartingale theory and stochastic calculus, Science Press, New York 1992.</p>
Example issues/ example questions/ tasks being completed	eResources addresses	<p>Podstawowe https://enauczanie.pg.edu.pl/moodle/course/view.php?id=31019 - Adresy na platformie eNauczanie:</p> <p>Discuss the construction of stochastic integrals with respect to local martingales with continuous paths.</p> <p>Give the general stopping theorem.</p> <p>Give the Ito formula and proved it.</p>
Work placement	Not applicable	

Document generated electronically. Does not require a seal or signature.