



Subject card

|  |  |  |                                     |            |  |         |     |
|--|--|--|-------------------------------------|------------|--|---------|-----|
| Subject name and code  | , PG_00052287  |  |                                     |            |  |         |     |
| Field of study   | Mathematics  |  |                                     |            |  |         |     |
| Date of commencement of studies  | October 2025   | Academic year of realisation of subject  |                                     |            | 2025/2026  |         |     |
| Education level  | second-cycle studies   | Subject group  |                                     |            | Specialty subject group<br>Subject group related to scientific research in the field of study  |         |     |
| Mode of study  | Full-time studies  | Mode of delivery   |                                     |            | at the university  |         |     |
| Year of study  | 1  | Language of instruction  |                                     |            | Polish   |         |     |
| Semester of study  | 2  | ECTS credits   |                                     |            | 4.0  |         |     |
| Learning profile   | general academic profile   | Assessment form  |                                     |            | assessment   |         |     |
| Conducting unit  | Divison of Dynamical Systems -> Institute of Applied Mathematics -> Faculty of Applied Physics and Mathematics -> Faculties of Gdańsk University of Technology   |  |                                     |            |  |         |     |
| Name and surname of lecturer (lecturers)   | Subject supervisor   |  | dr hab. Sergey Kryzhevich           |            |  |         |     |
|  | Teachers   |  | dr hab. Sergey Kryzhevich           |            |  |         |     |
| Lesson types   | Lesson type  | Lecture  | Tutorial                            | Laboratory | Project  | Seminar | SUM |
|  | Number of study hours  | 30.0   | 0.0                                 | 0.0        | 0.0  | 30.0    | 60  |
|  | E-learning hours included: 0.0   |  |                                     |            |  |         |     |
| eNauczanie source address: <a href="https://enauczanie.pg.edu.pl/2025/course/edit.php?id=5221">https://enauczanie.pg.edu.pl/2025/course/edit.php?id=5221</a> |  |  |                                     |            |  |         |     |
| Learning activity and number of study hours  | Learning activity  | Participation in didactic classes included in study plan   | Participation in consultation hours |            | Self-study   | SUM     |     |
|  | Number of study hours  | 60   | 5.0                                 |            | 35.0   | 100     |     |
| Subject objectives   | Introduction to basic tools and methods related to the theory of systems of nonlinear ordinary differential equations.   |  |                                     |            |  |         |     |
| Learning outcomes  | Course outcome   | Subject outcome  |                                     |            | Method of verification   |         |     |
|  | [K7_U07] at an advanced level and covering modern mathematics, applies and presents in speech and in writing the content and methods of a selected branch of mathematics   | The student is able to solve autonomous linear systems and some nonlinear integrable systems.  |                                     |            | [SU1] Assessment of task fulfilment<br>[SU4] Assessment of ability to use methods and tools  |         |     |
|  | [K7_K02] formulates questions to deepen own understanding of a given topic or find missing elements of reasoning, understands the need to clearly present selected achievements of higher mathematics to laymen. | The student knows and is able to apply basic facts from stability theory and some numerical methods for solving nonlinear systems.   |                                     |            | [SK3] Assessment of ability to organize work<br>[SK4] Assessment of communication skills, including language correctness<br>[SK5] Assessment of ability to solve problems that arise in practice |         |     |
|  | [K7_W01] has enhanced knowledge of basic branches of mathematics, demonstrates knowledge theorem and hypotheses, has understanding of the role and importance of mathematical reasoning structure.               | The student is able to apply basic methods of linear algebra, mathematical analysis, functional analysis and other mathematical disciplines to solve systems of nonlinear ordinary differential equations or to carry them out for qualitative analysis. |                                     |            | [SW1] Assessment of factual knowledge<br>[SW2] Assessment of knowledge contained in presentation   |         |     |

|  |   |  |                               |
|--|---|--|-------------------------------|
| Subject contents   | Course content – lecture  |  |                               |
|  | 1) General properties of nonlinear systems. Existence and uniqueness of solutions.<br>2) Homogeneous and inhomogeneous linear systems.<br>3) Fundamental matrices, Wronski determinants.<br>4) Systems with constant coefficients. Matrix exponents.<br>5) Euler's method.<br>6) Inhomogeneous systems and methods for solving them.<br>7) Dependence on initial conditions and parameters.<br>8) Stability.<br>9) Lyapunov functions.<br>10) Types of fixed points in the plane. |  |                               |
|  | Course content – seminar<br>The program of seminarium is similar.   |  |                               |
| Prerequisites and co-requisites                                | Knowledge of subjects: Algebra, Analysis, Ordinary Differential Equations.  |  |                               |
| Assessment methods and criteria                                | Subject passing criteria  | Passing threshold  | Percentage of the final grade |
|  | Exercises   | 51.0%  | 50.0%                         |
|  | Exam  | 51.0%  | 50.0%                         |
| Recommended reading  | Basic literature  | 1.W. Żakowski, W. Leksiński, Matematyka, Część IV, Warszawa, 1995.<br><br>2. M. Gehwert, Z. Skoczylas, Równania różniczkowe zwyczajne: teoria, przykłady, zadania, Wrocław, 2001.          |                               |
|  | Supplementary literature  | 1. R.S. Guter, A.N. Janpolski, Równania różniczkowe, PWN, Warszawa, 1980.<br><br>2. W.I. Smirnow, Matematyka Wyższa, Tom II, PWN, Warszawa, 1966.  |                               |
|  | eResources addresses  | Basic<br><a href="https://caiomp-zchdn7o2dcaci7ei4p8lnc.vpn.pg.edu.pl/2025/course/view.php?id=5221">https://caiomp-zchdn7o2dcaci7ei4p8lnc.vpn.pg.edu.pl/2025/course/view.php?id=5221</a> - |                               |
| Example issues/<br>example questions/<br>tasks being completed | Students complete test works. Theoretical knowledge acquired in lectures and seminars is assessed in an exam.<br>Example questions.<br>1) State and prove the properties of the matrix exponent.<br>2) State and prove the fixed point stability theorem.<br>3) Determine the type of fixed points for a system of two equations.   |  |                               |
| Practical activities within the subject                        | Not applicable  |  |                               |

Document generated electronically. Does not require a seal or signature.