



Subject card

Subject name and code	Mathematics, PG_00054686						
Field of study	Biotechnology						
Date of commencement of studies	October 2026	Academic year of realisation of subject			2026/2027		
Education level	first-cycle studies	Subject group			Obligatory subject group in the field of study		
Mode of study	Full-time studies	Mode of delivery			at the university		
Year of study	1	Language of instruction			Polish		
Semester of study	2	ECTS credits			9.0		
Learning profile	general academic profile	Assessment form			exam		
Conducting unit	Mathematics Center -> Vice-Rector For Education						
Name and surname of lecturer (lecturers)	Subject supervisor		dr Anita Dąbrowicz-Tłałka				
	Teachers						
Lesson types	Lesson type	Lecture	Tutorial	Laboratory	Project	Seminar	SUM
	Number of study hours	45.0	45.0	0.0	0.0	0.0	90
	E-learning hours included: 0.0						
Learning activity and number of study hours	Learning activity	Participation in didactic classes included in study plan		Participation in consultation hours		Self-study	SUM
	Number of study hours	90		10.0		125.0	225
Subject objectives	The aim of this subject is to obtain the students competence in the range of using the basic methods of mathematical analysis and linear algebra. Furthermore, the student is able to use this knowledge to solve simple theoretical and practical problems that can be found in the field of engineering.						
Learning outcomes	Course outcome		Subject outcome		Method of verification		
	K6_U01		Student uses gained knowledge in basic mathematics to analyse results of experiments .		[SU2] Assessment of ability to analyse information [SU1] Assessment of task fulfilment		
	K6_W01		Student examines the convergence of the number series. Student defines basic notions of matrix calculus. Student uses basic notions and formulas of matrix calculus in solving systems of linear equations. Student analyses properties of a given function of two variables using differential calculus of several variables functions. Student uses double and triple integral in geometrical applications. Student determines gradient, divergence and rotation as well as field potential. Student demonstrates some chosen techniques of solving ordinary differential equations. Student gives the definition of basic notions of probability theory. Student describes the basic types of distributions of random variable.		[SW1] Assessment of factual knowledge		

Subject contents	<p>Course content – lecture Providing theoretical knowledge, linking it to material already covered, and analyzing examples of the use of knowledge and skills in tasks related to:</p> <p>Number series: Convergent and divergent series. Convergence tests of the number series.</p> <p>Elements of linear algebra: Matrices, their properties and operations on matrices. Determinants. Inverse of a square non-singular matrix. Dot product, cross product, their properties and its applications. The triple scalar product and applications.</p> <p>Systems of linear equations. Cramer patterns. The rank of the main and completed matrix. Kronecker-Capelli theorem.</p> <p>Functions of two variables: Partial derivatives. Total differential.</p> <p>Taylor's formula. Maxima and minima of a function of several variables.</p> <p>Multiple integrals: Normal and regular area. Double and triple integral. Change of variables - polar, cylindrical and spherical coordinates. Examples of applications.</p> <p>Elements of field theory: scalar and vector fields. Gradient, divergence, rotation.</p> <p>Ordinary differential equations: First order linear differential equations. Linear differential equations order n with constant coefficients.</p> <p>Calculus of probability: Discrete and continuous random variable, distribution function, expected value and variance of a random variable. Basic distribution of a random variable.</p> <hr/> <p>Course content – exercises Tasks involving the selection of criteria for determining the convergence or divergence of numerical series. Using matrix properties and matrix operations to solve matrix equations and calculate determinants. Exercises in applying the properties of vectors, scalar products, vector products, and mixed products. Determining methods for solving systems of linear equations using Cramer's formulas, Kronecker-Capelli's theorem, and Gauss's elimination method. Exercises in determining partial derivatives, calculations in the field of applications (extrema and gradient, divergence, rotation, potential). Tasks related to calculating double integrals, representing areas in polar coordinates, solving tasks from selected applications of double integrals. Solving ordinary differential equations - general and specific solutions, Cauchy's initial value problem. Correct identification of the type of equation and application of the appropriate method: equations with separated variables, first-order linear differential equations, second-order linear differential equations with constant coefficients. Exercises in determining probability distribution functions, distributives for discrete and continuous random variables. Determining probability, expected value, variance, and standard deviation. Examples of random variables and their distributions.</p>																	
Prerequisites and co-requisites																		
Assessment methods and criteria	<table border="1"> <thead> <tr> <th data-bbox="456 1547 794 1576">Subject passing criteria</th> <th data-bbox="799 1547 1137 1576">Passing threshold</th> <th data-bbox="1142 1547 1481 1576">Percentage of the final grade</th> </tr> </thead> <tbody> <tr> <td data-bbox="456 1583 794 1612">class work</td> <td data-bbox="799 1583 1137 1612">0.0%</td> <td data-bbox="1142 1583 1481 1612">10.0%</td> </tr> <tr> <td data-bbox="456 1619 794 1648">midterm tests</td> <td data-bbox="799 1619 1137 1648">0.0%</td> <td data-bbox="1142 1619 1481 1648">40.0%</td> </tr> <tr> <td data-bbox="456 1655 794 1684">written exam</td> <td data-bbox="799 1655 1137 1684">50.0%</td> <td data-bbox="1142 1655 1481 1684">45.0%</td> </tr> <tr> <td data-bbox="456 1691 794 1720">oral exam</td> <td data-bbox="799 1691 1137 1720">50.0%</td> <td data-bbox="1142 1691 1481 1720">5.0%</td> </tr> </tbody> </table>			Subject passing criteria	Passing threshold	Percentage of the final grade	class work	0.0%	10.0%	midterm tests	0.0%	40.0%	written exam	50.0%	45.0%	oral exam	50.0%	5.0%
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Recommended reading	Basic literature	<p>- M. Gewert, Z. Skoczylas : Analiza matematyczna 2, Oficyna Wydawnicza GiS, Wrocław;</p> <p>- K. Jankowska, T. Jankowski : Zadania z matematyki wyższej, Wydawnictwo PG, 2010;</p> <p>- K. Jankowska, T. Jankowski : Funkcje wielu zmiennych - Całki wielokrotne - Geometria analityczna, Wydawnictwo PG, 2010;</p> <p>- E. Mieloszyk : Macierze, wyznaczniki i układy równań, Wydawnictwo PG, 2000;</p> <p>- M. Bednarczyk, A. Dąbrowicz-Tlałka, Wdawnictwo PG, 2016</p>
	Supplementary literature	<p>G.M. Fichtenholz : Rachunek różniczkowy i całkowy, t. 2, Wydawnictwo Naukowe PWN</p> <p>W. Krywicki, L. Włodarski : Analiza matematyczna w zadaniach II, Wydawnictwo Naukowe PWN</p> <p>R. Leitner, Zarys matematyki wyższej II, Wydawnictwo Naukowo-Techniczne</p> <p>W. Stankiewicz : Zadania z matematyki dla wyższych uczelni technicznych, Wydawnictwo Naukowe PWN</p>
	eResources addresses	
Example issues/ example questions/ tasks being completed	<ol style="list-style-type: none"> 1. Check the convergence of the series ... and determine its type. 2. Discuss the solvability of the given system of equations 3. Find local extrema of the given function $f(x, y) = \dots$ 4. Using a double or triple integral, find the volume of a solid bounded by surfaces.... 5. Determine the potential of the vector field... 6. Using the prediction method, solve the first and second order linear differential equations. 7. Calculate the expected value and variance of the given random variable of the continuous type ... 	
Practical activities within the subject	Not applicable	

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